10.1029/2019TC005933 Item availability restricted. file

Publishers page: http://dx.doi.org/10.1029/2019TC005933
<http://dx.doi.org/10.1029/2019TC005933>

Please note:
Changes made as a result of publishing processes such as copy-editing, formatting and page numbers may not be reflected in this version. For the definitive version of this publication, please refer to the published source. You are advised to consult the publisher’s version if you wish to cite this paper.

This version is being made available in accordance with publisher policies. See http://orca.cf.ac.uk/policies.html for usage policies. Copyright and moral rights for publications made available in ORCA are retained by the copyright holders.
Evidence from high resolution topography for multiple earthquakes on high slip-to-length fault scarps: the Bilila-Mtakataka fault, Malawi

M. Hodge¹, J. Biggs², Å. Fagereng¹, H. Mdala³, L. Wedmore², J. Williams¹

¹School of Earth and Ocean, Cardiff University, UK
²School of Earth Sciences, University of Bristol, UK
³Geological Survey Department, Malawi

Key Points:

• We use satellite topography and a numerical model to analyse normal fault scarps and knickpoints potentially reflecting multiple earthquakes
• The Bilila-Mtakataka fault, Malawi, shows evidence for at least two previous ruptures with up to 10-12 m of vertical offset each.
• The degradation of the scarps suggests a diffusion age of 48±25 m² corresponding to 6.4 ± 4.0 kyr since formation.

Corresponding author: Juliet Biggs, juliet.biggs@bristol.ac.uk
Abstract

Geomorphological features such as fault scarps and stream knickpoints are indicators of recent fault activity. Determining whether these features formed during a single earthquake or over multiple earthquakes cycles has important implications for the interpretation of the size and frequency of past events. Here, we focus on the Bilila-Mtakataka fault, Malawi, where the 20 m high fault scarps exceed the height expected from a single earthquake rupture. We use a high resolution digital elevation model (<1 m) to identify complexity in the fault scarp and knickpoints in river profiles. Of 39 selected scarp profiles, 20 showed evidence of either multi-scarps or composite scarps and of the seven selected river and stream profiles, five showed evidence for multiple knickpoints. A near uniform distribution of vertical offsets on the sub-scarps suggests they were formed by separate earthquakes. These independent methods agree that at least two earthquakes have occurred with an average vertical offset per event of 10 and 12 m. This contrasts earlier studies which proposed that this scarp formed during a single event, and demonstrates the importance of high-resolution topographic data for understanding tectonic geomorphology. We use a one-dimensional diffusion model of scarp degradation to demonstrate how fault splays form multi-scarps and estimate the diffusion age $\kappa t$ of the Bilila-Mtakataka fault scarp to be $48 \pm 25$ m$^2$, corresponding to $6400 \pm 4000$ years since formation. We calculate that a continuous rupture would equate to a $M_W 7.8 \pm 0.3$ earthquake, greater than the largest seismic event previously recorded in East Africa.

1 Introduction

Historical and instrumental catalogues alone provide a short and incomplete record of past earthquakes (e.g. McCalpin, 2009; Hodge et al., 2015), and devastating earthquakes may occur on faults that have no historical earthquake activity (e.g. 2003 $M_W 6.6$ Bam earthquake in Iran; Fu et al., 2004). By investigating fault-generated landforms such as fault scarps, an assessment of the earthquake and rupture history along a fault, and the probability and hazard of future earthquakes, can be made (e.g. Wallace, 1977; Duffy et al., 2014; Zhang et al., 1991; Bucknam & Anderson, 1979; Zielke et al., 2015; Nash, 1980; Hanks et al., 1984; Andrews & Hanks, 1985). Paleoseismological trenching can provide information about timing and magnitude of prehistoric earthquakes (e.g. Schwartz & Coppersmith, 1984; Michetti & Brunamonte, 1996; Palyvos et al., 2005), but trenching requires particular geomorphic conditions and is limited by site accessibility.

Estimates of the displacement and age of earthquake ruptures can be made from geomorphological analyses of fault scarps and river channels (e.g. Bucknam & Anderson, 1979; Avouac, 1993). The latest generation of satellite-derived Digital Elevation Models (DEMs) have sufficient resolution for these estimates to be made remotely (Figure 1). In cases where there are subtle changes in morphology, such as slope breaks within the fault scarp, the existence of multiple ruptures can be analysed (Wallace, 1980, 1984) for comparison with other paleoseismological records (Ewiak et al., 2015). Furthermore, along-strike comparisons, which are not possible with point sampling methods such as trenching, can be used to analyse the structural evolution of the fault (e.g. Perrin et al., 2016a; Cronce & Haller, 1991; Manighetti et al., 2005; Hodge et al., 2018b, 2019). Rivers and streams crossing fault scarps may also preserve indicators of past earthquakes in the form of vertical steps - called knickpoints - in an otherwise convex and smooth longitudinal profile (e.g. Ouchi, 1985; Holbrook & Schumm, 1999; Wei et al., 2015; Burbank & Anderson, 2011). These can be used to identify active fault traces in regions with complex topography (Litchfield et al., 2003), and for paleoseismological analysis (Wei et al., 2015; Ewiak et al., 2015).

In this study, we investigate whether indicators of multiple ruptures exist along two major structural segments of the Malawi Rift’s Bilila-Mtakataka fault (BMF). Earlier studies suggested that the scarp may reflect a single earthquake that ruptured the whole
Figure 1. Various geomorphic indicators of multiple ruptures in an idealized system assuming no lithological contrasts or bedrock fabric. a) A single rupture scarp, where the upper original surface (US) and lower original surface (LS) are separated by a scarp formed of a steep free face, and wash and debris faces. The elevation profile (red line) shows two prominent changes in slope marked by breaks in slope (white circles). b) A degraded scarp. Erosion and deposition of material smoothes the scarp surface. Following another surface rupture, either: c) A composite scarp forms, where the most recent rupture is indicated by a steeper slope on the scarp surface; or d) A multi-scarp forms where individual scarps are separated by a break in slope. These may form in either single or multiple earthquakes. e) A knickpoint forms during a rupture. f) Between rupture events the knickpoint retreats upstream. g) Another knickpoint forms following a subsequent rupture. The knickpoints are separated by reaches of the river which are at their equilibrium gradient.
along-strike extent of the fault (Jackson & Blenkinsop, 1997). However, more recent studies indicate that the fault scarp has a higher degree of along-strike structural complexity and actually consists of at least six geometrically distinct segments (Goda et al., 2018; Hodge et al., 2018b). UAV data collected on recent field visits also show that the scarp is more complex than previously described, at least in the few accessible localities.

Here we use a very high resolution (< 1 m) point cloud and DEM to detect changes or breaks in slope on individual scarp profiles and use knickpoint analysis to estimate the number of ruptures that may have occurred on each segment. In addition, we use the fault scarp morphology and knickpoint height to estimate the surface offset associated with each event. We then apply a model of scarp degradation to estimate the diffusion age $\kappa t$ of the scarp profiles, i.e. the amount of erosion that has occurred at the scarp’s crest since the scarp’s formation. Diffusion age $\kappa t$, having dimension [length]$^2$, is the product of diffusivity and chronological age (Andrews & Hanks, 1985). If we assume the diffusivity is constant, this allows us to infer the relative timing of each rupture, and by selecting a typical diffusion constant $\kappa$ of the region, we can convert diffusion age to chronological age $t$. Finally, we discuss the processes that formed the current BMF scarp and consider future rupture scenarios.

2 Geomorphic indicators of multiple ruptures

2.1 Complex fault scarps

The morphology of a fault scarp is dependent on many factors, including the type of earthquake, amount of slip, and the material properties of the surface it displaces. Typically, a single rupture fault scarp will comprise a free face whose gradient is greater than the angle of repose of the hillslope sediments (Figure 1a; e.g. Wallace, 1977; Nash, 1984; Lin et al., 2017). These distinctive free faces, however, erode away within a few hundred years (e.g. Bucknam & Anderson, 1979; Nash, 1984; Wallace, 1980), forming smoother, degraded scarp profiles (Figure 1b). When more than a single surface rupture has oc-
curred along a fault, the scarps may comprise either a single scarp face with differing slopes within it, or an array/stack of multiple discrete scarps set back from one another (Wallace, 1977; Nash, 1984; Crane & Haller, 1991; Zhang et al., 1991; Ganas et al., 2005). Composite scarps comprise a single band of oversteepened terrain where vertical offsets have accumulated onto the same slope over multiple earthquake cycles (Figure 1c; e.g. Zhang et al., 1991; Ganas et al., 2005), whereas the vertical offsets of multi-scarps are horizontally offset by terraces (e.g. Nash, 1984; Crane & Haller, 1991). Composite fault scarps develop when near surface slip is confined to the same fault plane, but multi-scarps form when slip is confined to a different near-surface fault splay during each earthquake event (e.g. Slemmons, 1957; Nash, 1984; Anders & Schlische, 1994; Kristensen et al., 2008). Both multi-scarps and composite scarps can exist along the same fault if a splay is re-activated as shown in the Serghaya Fault Zone, Syria (Gomberg et al., 2001), the northern Upper Rhine Graben, Germany (Peters & van Balen, 2007) and northern Baja California, Mexico (e.g. Mueller & Rockwell, 1995).

Multiple surface ruptures on composite scarps may be identified by changes in scarp slope, marked by slope breaks on the scarp’s elevation profile (Figure 1c; e.g. Nash, 1984; Lin et al., 2017); however, as the scarp degrades, these multiple rupture markers will disappear over time (e.g. Buckman & Anderson, 1979; Nash, 1984; Wallace, 1980). The terraces between individual scarps on a multi-scarp (Figure 1d; e.g. Mayer, 1982) provide a more lasting record of earthquake activity, but multi-scarps too are considered to degrade to a morphology similar to a degraded single rupture fault scarp over sufficient timescales (e.g. Nash, 1984; Andrews & Hanks, 1985). Understanding whether multiple earthquake ruptures have occurred on a fault scarp is important as surface displacements may be used in quantifying paleomagnitude estimates for faults (e.g. Wei et al., 2015; Swan et al., 1980; Walker et al., 2015), and overestimating slip per earthquake will influence recurrence interval calculations, and thus the inferred seismic hazard (e.g. Middleton et al., 2016).

2.2 Knickpoints

The offset produced by surface ruptures also generates a change in fluvial systems. Studying the topographical variations within bedrock rivers has been an effective tool in understanding the evolution of tectonically active landscapes (e.g. Finlayson et al., 2002; Montgomery & Brandon, 2002). In fluvial geomorphology, the change in the appearance of a river’s longitudinal profile can be a response to tectonic activity (e.g. Ouchi, 1985; Holbrook & Schumm, 1999; Litchfield et al., 2003; Wei et al., 2015; Burbank & Anderson, 2011). Typically, the longitudinal profile is smooth and concave in appearance; however, in bedrock channels, surface ruptures can produce knickpoints (Figure 1e; e.g. Wallace, 1977; Yang et al., 1985; Commins et al., 2005; He & Ma, 2015; Sun et al., 2016). Over time, knickpoints retreat upstream from their original position during the process of channel regrading (Figure 1f). As knickpoints migrate upstream they reduce in height, and may eventually disappear (Holland & Pickup, 1976). Subsequent surface ruptures can cause additional knickpoints to develop, separated by reaches of the river which are at their equilibrium gradient (Figure 1g).

If the retreat rate is known, the age of formation can be calculated by measuring the retreat distance, and the knickpoint height may be used (assuming rupture area is known) to estimate the magnitude of each earthquake event (e.g. He & Ma, 2015; Rosenbloom & Anderson, 1994; Sun et al., 2016; Castillo, 2017; Wei et al., 2015). However, numerical models and field observations have shown that many complex processes including sediment flux, channel morphology, channel slope and drainage area contribute to the rate of knickpoint retreat (Attal et al., 2008; Cowie et al., 2006; Attal et al., 2011; Whittaker et al., 2007b, 2007a; Gasparini et al., 2006). In the past, analysis of knickpoints was a field-based exercise (e.g. Yang et al., 1985; Rosenbloom & Anderson, 1994); however, by using high resolution DEMs and mathematical models, knickpoints can be
Figure 3. Scarp degradation model for soil-mantled fault scarps. a) Parameters used to generate a catalogue of synthetic fault scarps. FW = Footwall. HW = Hanging-wall. b) Parameters used for the degradation of a fault scarp profile using a one-dimensional diffusion equation.

identified using slope-area relationships and stream gradient calculations (e.g. Howard & Kerby, 1983; Bishop et al., 2005; Hayakawa & Oguchi, 2006, 2009).

3 Numerical model for the formation of multi-scarps

Numerical models of fault scarp diffusion have been used to explore the degradation of composite fault scarps (Avouac & Peltzer, 1993) on the assumption that erosion is transport-limited as would be the case for soil-mantled landscapes (Arrowsmith et al., 1998). However, the morphological changes caused by the degradation of multi-scarps is less well known. Here, we illustrate how the interplay between co-seismic surface offsets and degradation causes the formation of multi-scarps using a numerical solution to the one-dimensional diffusion equation (e.g. Culling, 1963; Nash, 1980; Hanks et al., 1984; Arrowsmith et al., 1998; Andrews & Hanks, 1985), which calculates changes in elevation $Z$ along a scarp profile (where $x$ is the horizontal distance) over time $t$ (Figure 3). Assuming the scarp erosion is transport-limited (where more debris is available for removal than processes are capable of removing), the vertical component of scarp degradation is governed by the conservation of mass, and can be applied using the equation (Smith & Bretherton, 1972):

$$\frac{dZ}{dt} = \kappa \frac{d^2Z}{dx^2}$$  \hspace{1cm} (1)

where $\kappa$ is the diffusion constant ($\text{m}^2/\text{kyr}$). Scarp degradation processes transport material from the crest of the fault scarp and deposit it at the base of the scarp, smoothing the scarp and reducing the average slope below the fault dip angle $\delta$ (Figure 3b). As the mechanical properties of bedrock are not considered by this equation, it is only strictly applicable to soil-mantled fault scarps.

In our model, an initial scarp is generated at distance $x_s$ along the profile assuming a down-dip, normal sense of displacement on a fault with dip $\delta$, following an earthquake of slip $u$ (Figure 3a). We assume an even slip distribution on the fault, including the surface offset and assume that the slope of the scarp and dip of the fault are equal following the rupture. By dividing the slip by the fault slip rate $r$, the time between ruptures $T_R$ can be found (also known as the recurrence interval, or return period). Between earthquakes, the scarp is degraded according to equation 1, and we chose a diffusion constant, $\kappa$ in the range of 5-10 $\text{m}^2/\text{kyr}$ suitable for sub-tropical climates. This lies between values proposed for semi-arid climates ($0.5-5 \text{ m}^2/\text{kyr}$; e.g. Hanks et al., 1984; Andrews...
The model simulation is run over a fixed period of time $T$, for a certain number of events. For multiple ruptures, model parameters ($u$, $r$, $\delta$, $x_s$ etc) may be fixed for the entire simulation period or varied per event. For the fixed parameter scenario, a fault scarp caused by a single rupture and a composite fault scarp generated by three smaller ruptures (on the same fault plane) both degraded to identical profiles after a certain diffusion age (Figure 4a,b). For a 60° dipping normal fault the transition from composite scarps to degraded scarp (i.e. when clear slope break points were removed) occurred at $\kappa t \sim 36$ m$^2$. For a 40° fault the transition occurred at $\kappa t \sim 20$ m$^2$. For $\kappa$ in the range of 5 and 10 m$^2$/kyr, this corresponds to a minimum of 2,000 years to create degraded scarps from composite scarps. Of course, this also depends on many factors that may have localised influences such as lithology, geological discontinuities (for example, joints), and moisture content.

Multi-scarps formed during variable parameter simulations which considered decreases in fault dip of $> 10^\circ$ per earthquake and changes to the active fault location, i.e. the formation of splays (Figure 4c-f). Moving the active fault plane toward the lower original surface created an asymmetric slope profile with a smoother tail toward the scarp top (Figure 4d), whereas the opposite was observed when the active fault was moved toward the upper original surface (Figure 4e). By alternating the active fault plane between two parallel surfaces, two composite scarps separated by a break in slope (i.e. a hybrid composite-multi-scarp) may develop (Figure 4f). The length between the base of one scarp and the crest of another was slightly smaller than the distance between faults due to the degradation of two scarp surfaces the terrace separates. These model results illustrate how degraded multi-scarp and composite scarps have a different morphological expression (Figure 4). This provides a theoretical framework in which normal fault multi-scarps can be interpreted, and we now move to an analysis of such scarps in a natural setting.

4 Data acquisition and processing

4.1 Tectonic setting of the Bilila-Mtakataka fault

The Malawi Rift is a 900 km long amagmatic section of the Western Branch of the East African Rift System (EARS; Ebinger et al., 1987; Ebinger, 1989). It consists of a series of ~100-150 km long grabens and half grabens, which are defined by basin bounding faults (Ebinger et al., 1987; Flannery & Rosendahl, 1990; Lao-Dávila et al., 2015). The northern and central parts of the Malawi Rift have been flooded by Lake Malawi, however, its three southernmost grabens are still exposed onshore (Dulanya, 2017; Hodge et al., 2019). Based on EARS-scale kinematic models, the Malawi Rift is currently accommodating ~2 mm/yr east-west extension for a fixed Nubian Plate reference frame (Saria et al., 2014; Stamps et al., 2018).

The BMF lies within the Makankijra Graben and extends for 110 km from the southern end of Lake Malawi to the northern end of the Zomba Graben (Figure 2a). The BMF is slightly oblique to the current extension direction but is considered to be pure normal as: (1) no strike-slip offsets have been observed in the field or in DEMs (Hodge et al., 2018a), and (2) it is broadly parallel to the structure that may have been the source of the 1989 Salima earthquake, which had a rake of -92°±25° and an epicentre 40 km north of the BMF’s surface expression (Jackson & Blenkinsop, 1993). This apparent dichotomy between its normal kinematics and slight obliquity to the regional extension direction can be explained by the presence of a deep-seated crustal weakness (Philippon & Hanks, 1985; Arrowsmith et al., 1996; Carretier et al., 2002; Kokkalas & Koukouvelas, 2005; Nivière & Marquis, 2000) and tropical climates (10 m$^2$/kyr; e.g. Zielke & Strecker, 2009). Estimates for $\kappa$ may also be affected by vegetation (Hanks et al., 1984). As expected a larger diffusion constant $\kappa$ causes more erosion and decreases the slope of the scarp.
Figure 4. The synthetic fault scarp formation and degradation. a) A single rupture scarp. b) A composite scarp formed by three equally-sized ruptures (R1, R2 and R3). Panels c-f) Multi-scars formed by: c) decreases in fault dip $\delta$ per rupture; d) movement of the active fault plane (solid red line) into the hanging-wall; e) movement of the active fault plane into the footwall; and f) alternating the active fault between two fault planes. The dashed lines denote the elevation (black) and slope (grey) profiles immediately following the rupture. The solid lines denote the profiles at the end of the recurrence interval $T_R$. 
et al., 2015; Hodge et al., 2018b), consistent with structural analysis that shows normal faults with a range of orientations can be reactivated within a uniform stress field (Williams et al., 2019).

The BMF juxtaposes amphibolite-grade Proterozoic gneisses and granulites in the footwall against post-Miocene sediments in the hanging wall (Walshaw, 1965; Jackson & Blenkinsop, 1997; Dulanya, 2017; Hodge et al., 2018b). The landscape is soil mantled, albeit with some rocky outcrops (Figure 5a-b). In contrast, river channels are rocky with little sediment remaining in the channels (Figure 5c-d). This is consistent with the standard assumptions for the geomorphological analyses performed here, namely that 1) degradation of the scarp is transport-limited and 2) retreat of the knickpoints is detachment-limited (Whipple & Tucker, 1999; Arrowsmith et al., 1998).

### 4.2 Data processing

To determine whether the Bilila-Mtakataka fault scarp records multiple earthquake events, as is qualitatively observed (Figure 6), we use a sub-metre point cloud generated from Pleiades imagery (Hodge et al., 2019). Because of the size of the point cloud (in excess of 30 GB), to save computational resources we restrict our study area to the two major segments at the centre of the BMF: the Mua and Kasinje segments (Figure 2b, S1) that are found to contain the largest scarps (> 20 m high) along the entire fault (Hodge et al., 2018b, 2019). Both the average height of these segments and the average scarp height (used as a proxy for vertical displacement; e.g. Morewood & Roberts, 2001) along the entire fault (∼ 14 m) exceed the magnitude of slip typical of a single event for a fault the length of the BMF (< 10 m; Scholz, 2002). Therefore, due to this and their central location along the BMF, the Mua and Kasinje segments may be the most likely segments to show evidence of multiple ruptures at the surface.

The BMF scarp is soil-mantled and the area surrounding it is densely vegetated (Figures 2b, 5a-b, 6 and S1), which causes significant, local fluctuations in elevation data (Hodge et al., 2019). When this noise propagates into slope calculations, it affects scarp parameter calculations, and so to analyse the sub-metre point cloud used in this study, we first improve the signal-to-noise ratio. To mask vegetation, a normalised difference vegetation index (NDVI) is calculated from the red (R) and near-infrared (NIR) bands (e.g. Elvidge & Lyon, 1985; Grigillo et al., 2012; Rawat & Joshi, 2012; Yu et al., 2011):

\[
NDVI = \frac{NIR - R}{NIR + R}
\]  

For 50 representative sample points, the median NDVI value for vegetated and non-vegetated areas was found to be 0.57 and 0.33, respectively (Figure S1). Non-vegetated areas were also found to have a larger composite RGB value than vegetated areas (i.e., they are lighter in RGB colour). The best performing NDVI threshold to reflect the transition to vegetation was 0.45, where just 4% of sample points were incorrectly identified (n=100, Figure S1). Note, this is higher than previous studies which have reported that a NDVI value greater than 0.2 coincides with vegetation coverage (Grigillo et al., 2012). However, this difference may be due to differences in camera calibration and colour levels. In addition, we manually remove additional large-scale noise features such as buildings that cannot be captured using the NDVI method.

### 4.3 Scarp profiles

Twenty-one scarp profiles along the Mua segment and eighteen from the Kasinje segment were identified as having a sufficient point cloud density (> 90% coverage and no gaps > 10 m) to be analysed (Figure S1). To account for geometrical variations along the segments influencing our vertical displacement calculations (e.g. Mackenzie & El-
Figure 5. Field photos of the Bilila-Mtakataka fault scarp (a-b) and knickpoints (c-d). a) Fault scarp along the Mua segment. b) Fault scarp along the Kasinge segment. White arrows indicate the base of the scarp, black arrows the top of the scarp. The scarps are soil mantled, with occasional rocky outcrops, consistent with the behaviour of hillslopes (and thus fault scarps) that erode in a diffusive manner. c) Knickpoint R1 along the Namikokwe River. d) Knickpoint R1 along the Mtuta River. The height of each knickpoint was estimated using photo analysis and corresponds well with the R1 knickpoint heights extracted from the Pleiades imagery (Figures 11 and 12). The rocky river channels shown here suggests that the retreat of these knickpoints is a detachment limited process.
Figure 6. Oblique views of the Bilila-Mtakataka fault scarp from a drone-based Digital Elevation Model. a) Naminkokwe River (Mua segment), b) Mtuta River (Kasinje segment). These images show local evidence for composite and multi-scarps. Knickpoints (kp) are clearly visible in both rivers.
liott, 2017), profiles were oriented to perpendicular to the average trend of the BMF (150°) (Hodge et al., 2018b). For each profile, points were taken at intervals of a half-metre. The minimum scarp profile length is 300 m.

Despite improving the signal-to-noise ratio, we find that local noise still results in variations in the gradient with an amplitude comparable to that expected by a scarp or knickpoint. To further improve the signal-to-noise ratio, we apply a digital filter to the elevation profiles. We use the rloess function in MATLAB as a filter, which is a more robust version of the Loess filter (Cleveland, 1981). The quadratic regression used by rloess is more computationally expensive than the Loess filter, but is better at removing outliers whilst not without drastically influencing the elevation or slope profiles (Hodge et al., 2019). As we do not want to artificially reduce the scarp slope or smooth over slope breaks, we choose a bin width of 15 m. Smaller window sizes failed to successfully eliminate background noise close to scarps.

4.4 River profiles

The rocky character of the rivers and streams in this area (Figure 5c-d) suggests knickpoint positions and retreat rates may encode information about the downstream faults tectonic history. The geological map by Dawson and Kirkpatrick (1968) shows the Naminkokwe River as the only major river that crosses the BMF scarp, but during fieldwork we identified two additional rivers that are suitable for knickpoint analysis: the Livelezi and Mtuta rivers (white circles Figure 2b). The Naminkokwe River is located at the northern end of the Mua segment (~37 km from the northern end of the fault). It is ~10 m wide on average, including where it crossed the fault scarp, but has a prominent 20 to 30 m wide section between 50 and 200 m from the scarp. The Livelezi River, which is located at the intersection between the Mua and Kasinje segments (near the town of Golomoti), is reasonably well-defined where it crosses onto the valley floor, comprising a width of around 20 m. Upstream the river is locally up to 100 m wide, but averages ~30 m. The larger channel width of the Livelezi River compared to the Naminkokwe River suggests it has a larger flow discharge (Leopold & Maddock, 1953). The Mtuta River, has a maximum width of ~10 m, but had significantly less discharge passing through it than the other rivers observed during fieldwork in the dry season. We identified 4 smaller unnamed channels using the DEM, and since these are <5 m wide, we refer to them as streams, and label them according to their location within the segment: Mua north, Mua South, Kasinje North and Kasinje South (grey circles, Figure 2b). During the fieldwork, no discharge passed through each stream. How discharge changes during the wet season for each river and stream is unknown to us currently.

Each channel was traced from the Pleiades point cloud using the polyline tool in CloudCompare®. The nearest point from the Pleiades point cloud to the polyline was selected within a parallel distance of 2 m, at an interval of a half-metre. The extracted point cloud was manually cleaned to remove noise. Because of smaller channel widths, the streams had more noise due to overhanging vegetation from the channel sides. This resulted in significant gaps in the extracted profiles for some streams. The points were then plotted along the length of the detailed channel, to form a two-dimensional profile where the horizontal axis is the distance from the fault scarp. As a smoothed longitudinal profile also better represents the true channel bottom (Wei et al., 2015), we apply a digital filter to improve the signal-to-noise ratio. As we want to preserve the vertical to sub-vertical gradients of the knickpoints to identify them in the river profiles, we use a Savitzky-Golay filter, which is based on local least-squares polynomial approximation (Savitzky & Golay, 1964) and helps preserve data features such as peak height and width. Due to the large elevation artefacts of the noise on the channels, we set the window size to be 20 m. Although all the channels show a clear downslope trend, there are sections that show a small, localised upslope trend, which is likely the result of vertical or horizontal uncertainty. The vertical uncertainty may be a few meters, especially where parts
of the scarp are far away from ground control points (GCPs) used to develop the DEM from the stereo-pair. Similarly, our polyline may not follow the true channel, for example, if there is a lower section adjacent to the selected point or there is overhanging vegetation cover that was not removed by the filter. However, these minor upslope trends could also be real, and may be overcome by the increased channel flow velocity and height during the wet season.

River drainage area is considered to be an important factor in the speed at which a knickpoint retreats through a river system (e.g. Berlin & Anderson, 2007; Seidl et al., 1994; Hayakawa & Oguchi, 2006; Bishop et al., 2005; Crosby & Whipple, 2006). We performed a hydrological analysis on a 30 m SRTM DEM in QGIS (Figure 2b) to compute drainage direction and discharge capacity (Figure 2c). A polygon was then drawn around the tributaries that drained into each river or stream at the point they incised the scarp to reflect the estimated drainage area (Figure 2c). As we are not certain of the hydrological processes acting over the Chirobwe-Ncheu fault to the west, and whether discharge flows over this fault and into the rivers or streams in this study, our polygons do not extend into the footwall of this fault. The results show that the Livelezi River has a drainage area in excess of 200 km$^2$, the Naminkokwe and Mtuta Rivers have drainage areas of 43 km$^2$ and 32 km$^2$ respectively, and the four smaller streams have drainage areas $< 20$ km$^2$.

5 Fault scarps

5.1 Scarp analysis methods

Using the characteristics typical of single or multiple surface ruptures on fault scarps (Figure 1), we categorise each profile as either: (i) a single rupture scarp, (ii) a degraded scarp, (iii) a composite scarp, or (iv) a multi-scarp. Scarp surfaces are marked by steep gradients and troughs in the calculated slope profile. Slope breaks are marked by gentle gradients separating multiple troughs. For composite scarps, the number of ruptures is quantified by the number of slope changes (i.e. pairs of major slope break points), and for multi-scarps, the number of slope breaks. We note that degraded scarps may be fault scarps that have experienced multiple ruptures, but have undergone sufficient degradation for individual rupture markers to be lost (e.g. Bucknam & Anderson, 1979; Nash, 1984; Wallace, 1980). As a result, for all scarp types the number of ruptures is a minimum estimate.

The total scarp height $H$ for each profile was calculated as the cumulative surface displacement along the fault (Figure 7a,b; Hodge et al., 2018b). First, the crest and base of the entire scarp (regardless of whether it contains multiple rupture indicators) were picked manually, then a regression line was fitted to the upper and lower original slopes. The scarp height is then calculated as the difference between the two regression lines at a location corresponding to the maximum slope on the scarp surface.

For multi-scarp profiles, the crest and base of each individual scarp surface (identified by breaks in slope) were manually picked and the scarp height of each calculated using the regression line method (Figure 7b). As scarps smooth over time due to degradation (e.g. Bucknam & Anderson, 1979; Nash, 1984; Wallace, 1980), and as the lithology along both segments is uniform at fault-scale (Walshaw, 1965; Hodge et al., 2018b) implying limited spatial variability in diffusivity, we order the scarp surfaces in terms of slope steepness: from steepest to gentlest. We then infer the steepest surface to be a less degraded, younger scarp surface and hence represent the most recent rupture event (R1), the next steepest surface to represent the next most recent rupture event (R2), and so forth. We note that the most recent surface rupture here denotes the most recent ‘observable’ surface rupture, where a more recent surface rupture may have occurred but may have been too small to identify, or eroded away. The horizontal distance between
scarp surfaces (i.e. between one scarp surfaces base and another’s crest) was also measured for multi-scarps.

For composite scarps, the scarp height of R1 ($H_{R1}$) - identified as the steepest scarp surface at the centre of the scarp - was calculated by fitting a regression line to the R2 surfaces and calculating the elevation difference at the location corresponding to the maximum slope on the R1 scarp surface (Figure 7a). The scarp height of earlier rupture events are then found by calculating the elevation difference ($Z$) using the regression line approach and the next older rupture surface, or original surfaces if calculating the oldest rupture, and subtracting the cumulative scarp heights of subsequent ruptures, i.e. $H_{Rn} = Z - \sum_{i=1}^{n-1} H_{Ri}$.

5.2 Results of scarp analysis

The average total scarp height for all profiles was 22±5 m; the average total scarp height for Mua profiles was slightly smaller (21 m) than Kasinje (22 m), but had a smaller standard deviation (6 m compared to 7 m, Figure 8c). On average, the total scarp height is larger at the centre of the segments than the edges, as has been previously observed (Hodge et al., 2018b, 2019). For several kilometres toward the intersegment zone (Livelezi River), the total scarp height for both segments decreases by up to 15 m; however, the local scarp height near the river increases by up to 10 m on both segments.

Figure 7c-h shows examples of degraded, composite and multi-scarps from the Mua and Kasinje segments. As no free faces were identified on any profile, none were categorised as a single rupture scarp (i.e., fresh scarp that formed in the last few decades). Profiles M5 and K16 are examples of degraded fault scarps, displaying a smooth elevation profile and symmetrical slope profile. M12 and K15 however show an increase in slope toward the scarp centre (highlighted green in Fig. 7e,f), typical of a recent rupture on a pre-existing scarp; these profiles are interpreted as composite scarps. Breaks in slope typical of multi-scarps can be found on M1 and K3, where the steepest scarp surface is shown in green in Fig. 7g,h.

Out of the 39 profiles, 19 were categorised as degraded scarps (nine on Mua, 10 on Kasinje), 14 as composite scarps (nine on Mua, five on Kasinje), and six as multi-scarps (three on both Mua and Kasinje). For multi-scarps, the steepest scarp surface (R1) was nearest the lower original surface for all but one profile (M1). For the 20 profiles where multiple events could be identified (i.e. composite scarps or multi-scarps), all but one showed evidence for two subscarps (R1 and R2, Figure 8b). The anomalous result, multi-scarp profile K12, has an additional break in slope (R3).

Our numerical model demonstrated that multi-scarps are formed by fault splays (Figure 4d-f), which is consistent with rupture of anisotropic rocks leading to the activation of different surfaces (e.g. Lee et al., 2002; Hodge et al., 2018b). Here, the majority of the multi-scarps on the two BMF segments were recorded at segment tips. This is consistent with fault splay formation at segment tips observed in other natural examples (Manighetti et al., 2001; Wu & Bruhn, 1994; Giba et al., 2012; Segall & Pollard, 1983), as well as experiments and theoretical models (Perrin et al., 2016a, 2016b; Willemse & Pollard, 1998).

For the degraded scarps, the average scarp heights were 21±5 m and 22±5 m, respectively for Mua and Kasinje. The total scarp heights for composite scarps and multi-scarps was ~23 m for both segments and therefore comparable to the average height of the degraded scarps. For composite scarps and multi-scarps, the scarp height of R1 was on average 11±2 m for the Mua segment, and 13±4 m for the Kasinje segment (green symbols, Figure 8a). For the Mua segment, the R1 scarp height was fairly constant, whereas it was more variable on the Kasinje segment and increased southward. The scarp related to R2 (orange symbols, Figure 8a) had a height of 12±4 m and 10±4 m for Mua and Kas-
Figure 7. Schematic showing a) composite scarp and b) multi-scarp profile. a) The scarp height of the most recent rupture event R1 ($H_{R1}$) is calculated by fitting a regression line to the maximum slope on the R1 scarp surface. The scarp height of a subsequent rupture event (i.e. $H_{R2}$) is then found by calculating the elevation difference ($Z$) using the regression line approach and the next older rupture surface, or original surfaces if calculating the oldest rupture, and subtracting the cumulative scarp heights of earlier ruptures (i.e. $H_{R1}$). b) Regression lines are fitted to the upper (US) and lower (LS) original surfaces, and the terraced surface (slope break) between scarps. The scarp height for each rupture event is then calculated as the elevation difference between regression lines at the slope maxima. c-h) Three examples from the Mua (c,e,g) and Kasinje segments (d,f,h): a degraded scarp with no indicators of multiple ruptures (c,d), a composite scarp with multiple events (e,f), and a multi-scarp with multiple rupture events (g,h).

Filled black triangles denote the crest of the entire fault scarp. Filled white triangles denote the scarp base. Filled grey triangles denote breaks or changes in slope between individual scarp surfaces formed by multiple ruptures. The steepest surfaces corresponding to R1 are coloured green, and the gentler surfaces corresponding to R2 are coloured orange.
Figure 8.  a) The total scarp height for scarp profiles (white filled), against individual scarp heights for the last rupture event (R1; green), penultimate rupture event (R2; orange), and third rupture event (R3; yellow), for scarp analyses. The box at the end of the profile shows the average (squares) and standard deviation (error bars) values for the scarp height of the following: total (black), degraded (grey), R1 (green), R2 (orange), and R3 (yellow). Knickpoint results are shown as stars corresponding to the inferred rupture event. b) The number of rupture events inferred from the scarp profiles (square = degraded scarps, diamond = composite scarps, circle = multi-scarps) and knickpoints (stars) for the Mua and Kasinje segments.

inje, respectively. The scarp height of R2 is greatest at the centre of the segments. A third subscarp (R3) on profile K12 was identified, comprising a scarp 5 m high.

5.3 Estimating diffusion age

Previous studies have applied the scarp degradation model shown in Figure 3 to natural fault scarps in soil-mantled landscapes. Using the slip and slip rate along a fault to estimate the date of the scarp-forming earthquake or earthquakes, it is possible to calculate the diffusion constant $\kappa$ (e.g. Avouac & Peltzer, 1993; Arrowsmith et al., 1998; Carretier et al., 2002). For the Bilila-Mtakataka fault, neither the date of past earthquakes nor the slip rate is known so we cannot directly estimate the diffusion constant $\kappa$. Instead we estimate the diffusion age $\kappa t$ (i.e. the amount of erosion that has occurred on the scarp since the earliest earthquake). Note, the term diffusion age is widely used in the literature but is misleading as it actually corresponds to the area given by the product of diffusivity $\kappa$ and chronological age $t$ (Andrews & Hanks, 1985). By making some assumptions about $\kappa$, we may then be able to convert $\kappa t$ to find the relative differences in age between scarp profiles.

We estimate the age of the 33 composite or degraded scarp profiles along the Mua and Kasinje segments shown in Figure 8a. As the negative change in elevation at the upper portion of the scarp should correspond to an equal positive change in elevation at the bottom of the scarp, only the erosion at the upper scarp needs to be calculated. First, the intersection is found between a regression line fitted to the upper surface and one...
fitted to the scarp surface. The two regression lines are then joined to reproduce the original scarp surface before degradation. Using equation 1 the initial scarp is degraded over a period of time of $T$ at intervals of $t$. We assume a fault dip of 60° in the absence of other information. At each step, the goodness of fit is assessed by comparing the modelled scarp profile against the observed scarp profile by estimating the root mean square error (RMSE). Confidence intervals are defined by considering profiles within a 5 cm range of RMSE$_{\text{min}}$ (Avouac & Peltzer, 1993; Arrowsmith et al., 1998).

The average diffusion age for the 33 scarp profiles is 48±25 m$^2$ with a range of ∼ 1 to 98 m$^2$. Minimum misfit (RMSE$_{\text{min}}$) between forward model and observations varies from less than 0.1 m (e.g., profiles M3, M17, K5 and K13) to ∼ 1 m (profile M9), with an average of ∼ 0.2 m. Profile M2 is an example of a reasonably well fitting profile (RMSE$_{\text{min}}$ ∼ 0.3 m) for a small diffusion age (11±8 m$^2$; Figure 9a). In comparison, profile K2 was estimated to have a similarly low diffusion age (16±5 m$^2$), but the model fit was worse (RMSE$_{\text{min}}$ 0.4 m, Figure 9b). The poor fit for profile K2 is due to the variable scarp slope near the scarp crest, a feature typical of composite scarps. In comparison profile M2 is a degraded scarp and therefore has a smoother slope profile. Profile M8 is an example of a scarp that has a large estimated diffusion age (98±17 m$^2$), where the fit between the model and observations were good but uncertainty was large (RMSE$_{\text{min}}$ 0.1 m, Figure 9c). The inverse solution of the model estimated a $\kappa t$ of just ∼ 1 m$^2$ for profile M9, but the RMSE$_{\text{min}}$ was ∼ 1 m, indicating a very poor fit.

In general, a better model fit was found for scarps with a larger diffusion age (Figure 10b). Of the 18 profiles whose $\kappa t$ is estimated to be less than 50 m$^2$, six have a RMSE$_{\text{min}}$ of 0.3 m or greater (M4, M9, M10, M11, K1 and K2), whereas only one profile has an equivalent RMSE$_{\text{min}}$ where $\kappa t$ is > 50 m$^2$ (M6). Smaller scarps typically have a smaller $\kappa t$ than larger scarps (Figure 10c). The smallest scarp (K16, ∼ 15 m high) has a $\kappa t$ of ∼ 24±7 m$^2$, whereas the largest scarp (M17, ∼ 31 m high) has a $\kappa t$ of ∼ 66±8 m$^2$. Profile M20 is the anomalous result to this relationship, where a ∼ 14 m high scarp has a $\kappa t$ of 80±17 m$^2$. This scarp is located within 5 km of the intersegment zone. Typically, Mua segment scarps close to the intersegment zone have larger estimated $\kappa t$ values than those at comparable distances on the Kasinje segment (Figure 10a).

The Mua and Kasinje segments have the same average $\kappa t$ value within error (Figure 10a). The estimated $\kappa t$ value for the Mua segment is 52±24 m$^2$ (n=18) and for the Kasinje segment is 42±26 m$^2$ (n=15). For both segments, degraded and composite scarps have a similar average diffusion age (∼ 50 m$^2$), but degraded scarps have a larger standard deviation. This may imply that there is no major difference in diffusion (or age) between the two types of scarps. Profiles M8 and K6 have the largest estimated diffusion age (95±20 m$^2$) and M2 and K4, the smallest (11±0 m$^2$, Figure 10a). This is likely due to the steep surface near the scarp crest, which the model could not fit a reasonable degraded surface to. Typically, $\kappa t$ values are lower at the segment ends than the centre, but variations do occur (Figure 10a).

6 Knickpoints

We calculate the gradient of each river profile using a rolling window of length $d$:

$$G_d = \frac{e_2 - e_1}{d} \quad (3)$$

where $e_1$ and $e_2$ are elevations at $d/2$ either side of the measurement point respectively. The value of $G_d$ changes as a function of $d$ in response to the local riverbed morphology (Wei et al., 2015). Here, we test a $d$ of 10 and 70 m and find that the best value for our data is $d = 10$ m, but large knickpoints could still be identified using $d = 70$ m (Figure 11). Attempts have been made to automate knickpoint identification using $G_d$.
Figure 9. Diffusion age ($\kappa t$) calculations for three selected examples: a) Profile M2 where a reasonable RMSE$_{\text{min}}$ (0.27) was found for a $\kappa t$ of 11±8 m$^2$, b) profile K2 where a large RMSE$_{\text{min}}$ (0.65) was found for a $\kappa t$ of 28±7 m$^2$, and c) profile M8 whose RMSE$_{\text{min}}$ of 0.23 shows a good model fit to a $\kappa t$ of 98±17 m$^2$. 
Figure 10. Diffusion ages $\kappa t$ for scarp profiles across the Mua and Kasinje segments of the Bilila-Mtakataka fault. a) the estimated $\kappa t$ plotted against the distance along the fault; b) RMSE$_{\text{min}}$ versus $\kappa t$, and c) total scarp height versus $\kappa t$. 
(Hayakawa & Oguchi, 2006); however, choosing an appropriate threshold value to objectively define knickpoints is challenging for small drainage areas (Wei et al., 2015). Here, we choose $G_d > 0.2$ and manually analyse smaller peaks.

To identify which knickpoints are caused by faulting, we follow the criteria proposed by Wei et al. (2015): 1) knickpoints are only considered if they are located upstream of the fault scarp (i.e. in the footwall); 2) we exclude candidates if the elevation fluctuates considerably on either side of the point; and 3) we use geological and topographical maps, to exclude points positioned at lithologic contacts, at the confluence of tributaries and/or bends in the river profile (Wohl, 1993). We note that regional geological maps may not account for local lithological variation, a possible source of error within the profiles. We number the knickpoints for each stream chronologically based on their distance from the scarp (i.e. $K_{p1}$, $K_{p2}$...$K_{pn}$).

Each river or stream has at least one inferred knickpoint, $K_{p1}$ (Figure 11). The first knickpoint is well defined, and is usually located within 100 m of the fault scarp. The larger distance of $K_{p1}$ on the Livelezi River ($\sim 900$ m) may suggest that the retreat rate on the Livelezi is faster than the others, consistent with its larger discharge rate (assumed by its larger width) and drainage area (Figure 12a; e.g., Berlin & Anderson, 2007; Scidl et al., 1994; Hayakawa & Oguchi, 2006; Bishop et al., 2005; Crosby & Whipple, 2006).

The river with the second largest drainage area/discharge is the Naminkokwe River (Dawson & Kirkpatrick, 1968), whose $K_{p1}$ is setback the second furthest from the scarp ($\sim 95$ m). A second knickpoint $K_{p2}$ was identified on five of the profiles (Naminkokwe and Mtuta rivers, both Mua streams and the northern Kasinje stream), but not on Livelezi River. Where identified, $K_{p2}$ is setback between 130 and 190 m from the scarp (Figure 11). A third knickpoint $K_{p3}$ was identified on both the Naminkokwe and Mtuta rivers and is setback 160 to 250 m from the scarp. The lack of additional knickpoints on the Livelezi River may be due to the larger catchment area and discharge rate causing knickpoints to migrate upstream at a faster rate, beyond the limits of our profile (Wallace, 1977; Whittaker et al., 2007b, 2007a, 2008; Attal et al., 2011, 2008).

To calculate the height of the knickpoints, we manually pick the top and bottom of the knickpoint, using the onset and end of the trough in the calculated profile gradient. Then we fit a regression line through the upper and lower surface and calculate the elevation difference between these regression lines at the centre of the knickpoint. The location of the knickpoint is measured as the distance upstream from the scarp. The average height of $K_{p1}$ (green stars, Figure 8b) was 12±3 m on the Mua segment and 13±3 m on the Kasinje segment. Additional knickpoints ($K_{p2}$ and $K_{p3}$) were typically lower, measuring around 5 m on average; however, $K_{p2}$ on the southern Kasinje stream measured 19 m in height, larger than the height of $K_{p1}$ measured along the stream (10 m).

The number of knickpoints corresponds well with number of sub-scarps identified on the scarp profiles, and confirms that more than one rupture event has likely occurred on both the Mua and Kasinje segments of the Bilila-Mtakataka (Figure 8b). The clustering of $K_{p1}$ suggests they were formed by the same event: the last rupture event (R1). Similarly, we attribute the similar distances of $K_{p2}$ on all profiles (Figure 12) to be due to a concurrent, or near concurrent, older rupture: the penultimate, observable surface rupturing event (R2). Along on the Naminkokwe and Mtuta rivers, which both have similar drainage areas (Figure 2), $K_{p3}$ are setback a similar distance. Furthermore, the knickpoint of the Mtuta River is situated a few kilometres south of where a third rupture event was found on scarp profile K12. Consequently, this third knickpoint may be representative of a potential third, older rupture (R3).
Figure 11. River and stream profiles for: a) Naminkokwe River; b) Mua north stream; c) Mua south stream; d) Livelezi River; e) Kasinje north stream; f) Kasinje south stream; and g) Mtuta River. Profile elevation (black circles) was filtered using the Savitzky-Golay digital filter and window size of 20 m. For the $G_d$ plot a $d$ of 10 (blue) and 70 m (red) were used to identify knickpoints. The dotted black line indicates a $G_d$ of 0.2. Knickpoints identified in the gradient $G_d$ profile are shown as grey triangles. These were then quality checked and considered tectonic knickpoints (green triangles) or artefacts of noise (orange triangles). Knickpoints are numbered $K_p1, K_p2$ etc based on their distance from the scarp.
Figure 12. a) Knickpoint distance from scarp versus drainage area. b) Knickpoint distance from scarp versus scarp height. Filled symbols are knickpoints deemed to tectonic knickpoints, whereas outlined symbols have been considered to be noise artefacts and have been removed from the analysis.

7 Discussion

7.1 Comparison between scarp and knickpoint analyses

Whereas previous analyses on the BMF have focused solely on the total scarp height (Hodge et al., 2018b, 2019), here using the high resolution DEM created from Pleiades data, we were able to identify sub-scarps and estimate the incremental vertical surface displacements. While it is possible that multiple splays were active during a single event, the consistent pattern of vertical displacements along the length of the segments suggests these sub-scarps record separate earthquakes rather than local variations in geometry. The average scarp height of the most recent rupture event (R1) was ~12 m on both segments. The penultimate rupture event (R2) identified from the composite and multi-scarps had a similar scarp height (~11 m). The R1 and R2 scarp height profiles show variability along the segments and there are significant gaps in where R2 was recorded due to noisy profiles. A third potential event recorded on K12 had a scarp height of 5 m, and it is likely that any evidence for older events will have been obscured by erosion. The total scarp heights broadly match previous results (Hodge et al., 2018b, 2019), and show that while there is an intense local variability in the scarp height along the BMF, the average total scarp height is over 20 m on both segments, and is largest at the segment centres (Figure 8).

The height of individual knickpoints that have formed during consecutive ruptures may be a proxy for the vertical offset in each earthquake (Wei et al., 2015). We compare the cumulative knickpoint height measured from each river profile to the total scarp height measured from the closest scarp profile and find that the river profiles on average express 80% of the total scarp height. When comparing R1 knickpoint and scarp heights, the knickpoints record over 100% of the scarp height; as scarp height is locally variable, the closest scarp used here may not represent a larger scarp local to the knickpoint. The good correlation between knickpoint and scarp heights suggests that the well-defined first knickpoints (K1) are therefore likely true reflections of the latest vertical surface displacement from the most recent rupture on the two segments. The height of R2 from the river profiles is between 20% and 50% of the nearest R2 scarp height, when not including the abnormally large K2 height on the southern Kasinje stream. However, the nearest scarp...
profiles were all composite scarps, which may comprise additional ruptures that have been masked. When compared the R2 knickpoint height to the closest R2 scarp height from multi-scarps, the knickpoints express between 55% and 80% of the vertical offset. The R3 knickpoint on the Mtuta River has a height that expresses 90% of the nearest R3 scarp height from a multi-scarp.

The abnormally large knickpoint height of second knickpoint (∼ 19 m) on the southern Kasinje stream, when compared to other Kp2 heights (< 5 m) may be explained by a localised displacement high during an older event, or the inability to distinguish multiple older ruptures. The nearest scarp profile was taken only a few hundred metres from the stream and shows evidence for an older rupture producing a ∼ 16 m high scarp (Figure 8). Because these profiles are from the centre of the Kasinje segment, this may imply that a larger displacement occurred here (conforming to a bell-shaped displacement profile); however, the large $\kappa t$ values from this region (Figure 10) may also suggest that older rupture markers may have been destroyed, and that the scarp and knickpoint R2 may be formed from multiple, older events. In addition, the small discharge and catchment area for the southern Kasinje stream means that if a subsequent ruptures did occur here, and did so within a short enough period of time, a break in the longitudinal profile between knickpoints may not have developed.

### 7.2 Age estimates

No historical rupture has been observed on the Bilila-Mtakataka fault, indicating that the most recent earthquake (R1) must have occurred over a hundred years ago (Midzi et al., 1999; Hodge et al., 2015). Our numerical model shows that even for regions with a small diffusion constant $\kappa$, a free face degrades and disappears within approximately a hundred years, consistent with our field and satellite observations. To remove individual event markers on composite scarps required $\kappa t$ larger than 20 m$^2$, corresponding to a total time since formation of at least two to four thousand years.

The estimated diffusion age of the Bilila Mtakataka scarp is 48±25 m$^2$, which corresponds to a total time since formation of 6.4±4.0 kyr, assuming a $\kappa$ of 7.5±2.5 m$^2$/kyr. Assuming a constant $\kappa$ for the entire scarp history may be invalid for regions where intense climatic variations occur over long timescales; however, drill cores from Lake Malawi suggest that the climatic conditions of Malawi have been relatively stable for the past 70,000 years (Scholz et al., 2011). The range of estimates might therefore imply that sections of the Mua and Kasinje segments are several thousand years older than others, and that the earlier earthquakes involved smaller segments rupturing independently. However, there was no correlation between diffusion age and scarp height (Figure 10c), nor is the distribution of knickpoints and scarp heights representative of multiple discontinuous ruptures. Instead we suggest that the wide variation in diffusion age is related to local erosional processes (i.e. variations in $\kappa$; e.g. Kokkalas & Koukouvelas, 2005) including variations in properties of the fault damage zone associated with differences in the cross-cutting relationship between the scarp trend and the gneissic foliation (Hodge et al., 2018b).

The diffusion age for the Mua (52 ± 24 m$^2$) and Kasinje (42 ± 26 m$^2$) segments is the same within error, implying the scarps likely formed at similar points in time. Similarly, the consistent height of the R1 scarp implies that it formed in a single event across both segments. The fact that the R1 height does not decrease at the end of our study area suggests that it also propagated north onto the Mtakataka segment and south onto the Bilila segment. In contrast, the height of R2 scarp decreases at both the segment ends and the intersegment zone, suggesting separate ruptures of the Mua and Kasinje segments. Even ruptures ~ 20 km in length with 10 m of surface displacement would imply an unusually large slip-length ratio $(5 \times 10^{-4})$ compared to global catalogues (Scholz, 2002).

We therefore suggest that the R2 event ruptured both segments concurrent - or near con-
current – in time, as supported by the similar diffusion ages. The lack of a displacement low between the segments from R1, as seen in R2, may suggest the segments have be-come more mature in their structural linkage over recent earthquake cycles. Our find-ings suggest therefore that the BMF segments, over the last two earthquake cycles, have not ruptured individually. This finding profoundly influences the seismic hazard of the area, as it implies that the rupture length is not constrained by the structural segment lengths (Goda et al., 2018).

### 7.3 Magnitude estimates

Using relationships between earthquake magnitude and the total average BMF scarp height (~14 m), previous studies had estimated that the scarp was formed by a $M_W$ 7.9 to 8.4 event (Jackson & Blenkinsop, 1997; Hodge et al., 2019). However, in this study we have concluded that the BMF scarp actually formed through multiple ruptures. Assuming that the whole BMF scarp reflects two earthquakes (i.e. any older events no longer contribute significantly to the scarp height), and that there was no vertical erosion be-tween these events, the average vertical displacement (i.e. throw) of each event is $7\pm4$ m. In using these surface measurements to estimate average coseismic displacement $D_s$ we note that it has been practice to infer $D_s$ both directly from throw (i.e. scarp height; Schwartz & Coppersmith, 1984; DuRoss, 2008; Nicol et al., 2010) or from projecting throw into the fault dip (Villamor & Berryman, 2001; Xu et al., 2018; Litchfield et al., 2018).

We apply both approaches here, noting that for a reasonable fault dip (60$^\circ$), our projected estimates of $D_s$ are only slightly increased ($8.1\pm5.2$ m).

Our new estimate of $D_s$ results in a slip-length ratio $\alpha$ of $6.8\pm5.5\times10^{-5}$ for a com-plete BMF rupture (rupture length, 110 km), which is in accordance with global values (Scholz, 2002). However, we cannot exclude the possibility that the most recent BMF earthquake ruptured only the Kasinje and Mua segments, in which case $D_s$ is 10 m, length $\sim$ 40 km, and thus $\alpha$ is $2.5 \times 10^{-4}$. Applying the methodology of Jackson and Blen-kinsop (1997) to calculate the magnitude of a complete BMF rupture, but with the re-vised value of $D_s$, we calculate a range of magnitudes from $M_W$ 7.7 to 8.3 (eq. 1, Ta-ble 1). Alternatively, we estimate the magnitude range for a complete BMF rupture of $M_W$ 7.3 to 7.9 according to the $D_s$–magnitude scaling law by Wells and Coppersmith (1994) (Table 1, eq. 2) and $M_W$ 7.8 to 9.1 according to the $D_s$–magnitude scaling laws for interplate dip-slip faults of Leonard (2010) (Table 1, eq. 3).

The Wells and Coppersmith (1994) magnitude estimates using $D_s$ are therefore com-parable to those estimated using their surface rupture length ($L$) scaling laws (Table 1, eq. 4), which range between $M_W$ 7.4 and 7.5 assuming a complete BMF rupture. How-ever, the Leonard (2010) $D_s$–magnitude scaling gives a larger $M_W$ than the $L$-magnitude scaling ($M_W$ 7.5, Table 1, eq. 5). This may be indicative of the fact that our estimates of $\alpha$ are either at the higher end of values proposed by Scholz (2002), or even greater; such high values of $\alpha$ have also been observed for other earthquakes, which like Malawi, are hosted in thick elastic crust (Rodgers & Little, 2006; Smekalin et al., 2010).

It is not possible to comment here further on which of the magnitude equations in Table 1 are most appropriate for the BMF, only to highlight the care that should be used when selecting earthquake scaling relationships (Stirling et al., 2013). Regardless, in ei-ther case, the estimated earthquake magnitude from a complete rupture of the BMF is slightly greater than the largest naturally recorded earthquake events on the EARS; the $M_W$ 7.3 1910 Rukwa event (Ambroseys & Adams, 1991), the $M_W$ 7.0 1990 Juba earth-quake (Hartnady, 2002), and the $M_W$ 7 2006 Machaze earthquake (Fenton & Bommer, 2006). Furthermore, the average $M_W$ of 7.8 for a complete BMF rupture is slightly lower than previously estimated (Jackson & Blenkinsop, 1997) and is another example of where better constraining rupture slip has led to lower magnitude estimates (e.g., the 1739 Yinchuan earthquake, China; Middleton et al., 2016).
Table 1. Earthquake magnitude (including lower and upper) estimates using $L = 110$ km ($\pm 2$ km), $D_s = 7$ m ($\pm 4$ m), $G = 30$ GPa ($\pm 5$ GPa, Stein and Liu (2009)), and $W = T_s/\delta$ (where seismogenic thickness $T_s = 30$ km $\pm 5$ km Jackson and Blenkinsop (1993), and dip $\delta = 60^\circ \pm 5^\circ$).


<table>
<thead>
<tr>
<th>Eq N°</th>
<th>Description</th>
<th>Equation</th>
<th>Average $M_W$</th>
<th>$M_W$ Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1)</td>
<td>Normal fault slip $^{[1][2]}$</td>
<td>$M_W = \frac{2}{3} \cdot \log(GD_sLW) - 6.05$</td>
<td>8.0</td>
<td>7.7 - 8.3</td>
</tr>
<tr>
<td>(2)</td>
<td>All slip type $^{[3]}$</td>
<td>$M_W = 6.93 + 0.82 \cdot \log(D_s)$</td>
<td>7.6</td>
<td>7.3 - 7.9</td>
</tr>
<tr>
<td>(3)</td>
<td>Interplate dip-slip $^{[4]}$</td>
<td>$M_W = 6.84 + 2.00 \cdot \log(D_s)$</td>
<td>8.5</td>
<td>7.8 - 9.1</td>
</tr>
<tr>
<td>(4)</td>
<td>All slip type $^{[3]}$</td>
<td>$M_W = 5.08 + 1.16 \cdot \log(L)$</td>
<td>7.5</td>
<td>7.4 - 7.5</td>
</tr>
<tr>
<td>(5)</td>
<td>Interplate dip-slip $^{[4]}$</td>
<td>$M_W = 4.40 + 1.52 \cdot \log(L)$</td>
<td>7.5</td>
<td>7.5</td>
</tr>
</tbody>
</table>

These calculations assume a characteristic earthquake model for the BMF, and whilst the geomorphological analysis in this study found no evidence for single segment ruptures along the Mua and Kasinje segments, multi-segment ruptures may occur across both segments but not the entire fault. For example, the Citsulo segment may be a barrier to rupture propagation (Hodge et al., 2018b). Such ruptures would have a lower earthquake magnitude, due to the shorter rupture length, but also have a shorter recurrence interval. Complete and segmented ruptures along the BMF pose different seismic hazards for the region (Hodge et al., 2015; Goda et al., 2018). A detailed geomorphological analysis on the remaining BMF segments (Ngodzi, Mtakataka, Citsulo and Bilila) is therefore required.

8 Conclusion

The $\sim 110$ km long Bilila-Mtakataka fault comprises a scarp whose average height ($\sim 14$ m) exceeds that which would have formed from a single event, given global slip-length scaling laws (e.g., Scholz, 2002). Indeed, the two central structural segments - the Mua and Kasinje segments - have scarps more than 20 m high in places. Previous work has suggested that scarps of similar heights form through multiple ruptures on the same fault plane (a composite scarp) or unique near-surface fault planes (a multi-scarp). Our numerical models of scarp diffusion show that multi-scarps and composite-scarps display differing morphological signatures.

By undertaking a geomorphological analysis of the fault scarps along the Mua and Kasinje segments, using a high resolution DEM, we suggest there is evidence for at least two ruptures. A separate knickpoint analysis on three rivers and four streams that cross the fault scarp agree with these findings. By calculating the individual vertical displacement of each rupture from the scarp and knickpoints, we estimate the average vertical surface displacement along the two segments to be $\sim 10$ m per rupture. Results from a scarp degradation model used to estimate diffusion age $\kappa t$ on each scarp profile, by finding a best fit to the current profile, imply that the most recent rupture was continuous across both structural segments, and that the penultimate rupture was concurrent, or near-concurrent, in time across both segments. Extrapolating these findings for the en-
tire BMF, we suggest that the surface slip per event is less than 10 m, as expected by
global slip-length scaling laws, and that a complete rupture would equate to a MT range
of 7.5 to 8.1. This is likely smaller than previously suggested for the fault, but greater
than the largest earthquakes recorded along the entire EARS. We have demonstrated
that high resolution satellite topography can be used to identify surface ruptures from
multiple earthquakes. This could be applied to other large, prehistoric normal fault scarps
whose scarp height exceeds what would be anticipated by a single earthquake event (Scholz,
2002). Candidates for this include the Kanda fault, Lake Rukwa (Vittori et al., 1997;
Macheyeki et al., 2007), the Nahef East fault, northern Israel (Mitchell et al., 2001), the
Wasatch fault zone faults, Utah (Swan et al., 1980; DuRoss et al., 2015) and the Dixie
Valley-Pleasant Valley faults (Zhang et al., 1991).

Acknowledgments

Michael Hodge is supported by the NERC GW4+ Doctoral Training Partnership (grant
code NE/L002434/1) and Centre for Observation and Modelling of Earthquakes, Volc-
ocanes and Tectonics (COMET). Juliet Biggs is supported by COMET and the NERC
Large Grant Looking into Continents from Space (LiCS, NE/K010913/1). Juliet Biggs,
Åke Fagereng, Luke Wedmore and Jack Williams are supported by the EPSRC Global
Challenges grant PREPARE (EP/P028233/1). Hassan Mdala acknowledges the Geo-
logical Survey Department, Malawi, for attaching him to the project. All authors acknowl-
ledge the Geological Survey Department, Malawi, for their assistance with fieldwork in
Malawi. Pleiades data were obtained using a small grant from COMET and the point
cloud data are available from opentopography.org: https://doi.org/10.5069/G92R3PSV
(Mua section) and https://doi.org/10.5069/G96H4FJ1 (Kasinje section). We thank Dan
Hobley and two anonymous reviewers for their helpful comments on drafts of this manuscript.

References

south of 20 N, 1900–1930. *Natural Hazards, 4*, 389–419. Retrieved from
http://link.springer.com/article/10.1007/BF00126646

10.1086/629661 doi: 10.1086/629661


in areas of active tectonics. *Journal of Geophysical Research, 101*(B3),
6255–6275. doi: 10.1029/95JB02583

of scarps formed by repeated slip events along the San Andreas Fault, Carr-
rizo Plain, California. *Journal of Geophysical Research Solid Earth, 103*(B5),
10141–10160.

Attal, M., Cowie, P. A., Whittaker, A. C., Hodge, D., Tucker, G. E., & Roberts,
G. P. (2011). Testing fluvial erosion models using the transient response of
bedrock rivers to tectonic forcing in the Apennines, Italy. *Journal of Geophysi-

Modelling fluvial incision and transient landscape evolution: Influence of dy-
namic Channel adjustment. *Journal of Geophysical Research: Earth Surface,

Avouac, J.-p. (1993). Analysis of Scarp Profiles: Evaluation of Errors in Mor-


