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Filamentary fragmentation in a turbulent medium

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ABSTRACT

We present the results of smoothed particle hydrodynamic simulations investigating the evolution and fragmentation of filaments that are accreting from a turbulent medium. We show that the presence of turbulence and the resulting inhomogeneities in the accretion flow play a significant role in the fragmentation process. Filaments that experience a weakly turbulent accretion flow fragment in a two-tier hierarchical fashion, similar to the fragmentation pattern seen in the Orion Integral Shaped Filament. Increasing the energy in the turbulent velocity field results in more sub-structure within the filaments, and one sees a shift from gravity-dominated fragmentation to turbulence-dominated fragmentation. The sub-structure formed in the filaments is elongated and roughly parallel to the longitudinal axis of the filament, similar to the fibres seen in observations of Taurus, and suggests that the *fray and fragment* scenario is a possible mechanism for the production of fibres. We show that the formation of these fibre-like structures is linked to the vorticity of the velocity field inside the filament and the filament's accretion from an inhomogeneous medium. Moreover, we find that accretion is able to drive and sustain roughly sonic levels of turbulence inside the filaments, but is not able to prevent radial collapse once the filaments become supercritical. However, the supercritical filaments that contain fibre-like structures do not collapse radially, suggesting that fibrous filaments may not necessarily become radially unstable once they reach the critical line-density.

Key words: stars: formation – ISM: clouds – ISM: kinematics and dynamics – ISM: structure.

1 INTRODUCTION

It has long been known that filaments play a role in the star formation process (Schneider & Elmegreen 1979). The recent observations by the Herschel Space Observatory have revealed that filaments are prevalent within molecular clouds and that star-forming cores are often embedded within them (André et al. 2010; Arzoumanian et al. 2013; Könyves et al. 2015; Marsh et al. 2016). The ubiquity of filamentary structures has led to numerous papers studying the effects their geometry has on stability and fragmentation (Ostriker 1964; Larson 1985; Inutsuka & Miyama 1992; Freundlich, Jog & Combes 2014; Clarke, Whitworth & Hubber 2016).

Previous work has shown that filaments are prone to fragmentation due to their geometry; small-scale density perturbations have time to collapse locally before global longitudinal collapse occurs (Pon, Johnstone & Heitsch 2011). Inutsuka & Miyama (1992) have performed an analytic perturbation analysis to investigate how small-scale density perturbations grow in equilibrium filaments. They find that the most unstable perturbation has a wavelength roughly four times the filament's diameter.

However, it is unlikely that a filament forms, stops accreting, relaxes to equilibrium and then proceeds to fragment. Instead, filament and perturbations will co-evolve during a non-equilibrium accretion stage until the filament becomes unstable and fragments. This scenario has been investigated in an earlier work, Clarke et al. (2016) (hereafter CWH16). Using numerical simulations to investigate the perturbation growth in an accreting filament, CWH16 find that the fastest growing mode is the result of a resonance between radial accretion and longitudinal oscillations. The dominant wavelength is given by

$$\lambda_{\text{DOM}} \sim 2\tau_{\text{CRIT}}a_0, \quad (1)$$

where τ_{CRIT} is the time at which the filament becomes radially unstable and a_0 is the isothermal sound speed.

This fastest growing mode continues to be the dominant mode in simulations seeded with perturbations at multiple wavelengths. Moreover, the fastest growing mode is linked to the environment of the filament, its temperature and its accretion rate. This allows observers to determine the age, τ_{AGE} and mean accretion rate, $\langle \dot{\mu} \rangle$, of a filament that is fragmenting in a roughly periodic manner,

$$\tau_{\text{AGE}} \geq \tau_{\text{CRIT}} \simeq \frac{\lambda_{\text{CORE}}}{2a_0}, \quad (2)$$

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and

$$\langle \dot{\mu} \rangle \simeq \frac{2a_0\mu}{\lambda_{\text{CORE}}}, \quad (3)$$

where λ_{CORE} is the measured core separation and μ is the filament's line-density.

Tafalla & Hacar (2015) have recently observed the star-forming filament L1495 in Taurus, and find that it can be decomposed into velocity-coherent sub-filaments, which they term 'fibres'. On the basis of these results, they propose that filaments first fragment into fibres and that these fibres then go on to fragment into cores, a model they call *fray and fragment*. Recent simulations by Smith, Glover & Klessen (2014) suggest that fibres do not form from the fragmentation of filaments, but rather form in the surrounding cloud and are then swept up by large-scale motions to form a single column density structure. At present it is unclear which mechanism is dominant, or what role fibres play in filamentary fragmentation.

In this paper, we present numerical simulations of initially sub-critical filaments that accrete from a turbulent medium. Unlike the simulations presented in CWH16 in which density perturbations were placed in the accretion flow, the simulations in this paper use a turbulent velocity field to seed density perturbations. In Section 2, we detail the simulation setup and the initial conditions used; in Section 3, we present the results of these simulations; in Section 4, we discuss the significance of these results and compare to previous work and observations; and in Section 5, we summarize our conclusions.

2 NUMERICAL SETUP

The simulations presented in this paper are performed using the smoothed particle hydrodynamics (SPH) code GANDALF (Hubber et al. in preparation). The simulations invoke both self-gravity and hydrodynamics, with an isothermal equation of state. The temperature, T_0 , is taken to be 40 K throughout so as to compare to the fiducial case presented in CWH16; this results in an isothermal sound speed of $\sim 0.37 \text{ km s}^{-1}$, assuming solar metallicity. Grad-h SPH (Price & Monaghan 2004) is implemented, with $\eta = 1.2$, so that a typical particle has ~ 58 neighbours.

Sink particles are implemented as described in Hubber, Walch & Whitworth (2013) using the sink creation density, $\rho_{\text{SINK}} = 10^{-15} \text{ g cm}^{-3}$. However, as well as the standard sink creation criteria described in Hubber et al. (2013), an additional criterion is used which mitigates the overproduction of sink particles in well-resolved clumpy accretion flows on to an existing sink particle. To understand this additional criterion, consider a region in an accretion flow that is gravitationally bound, and an SPH particle, i , in it that satisfies all of the standard sink creation criteria. However, if this region is moving towards an existing sink particle, j , it may be accreted by sink j before the region's free-fall time has elapsed. If such a region is replaced with a new sink particle, one would end up with two smaller sink particles where there ought to be only one large sink particle. Thus, a candidate SPH particle's free-fall time must be less than the accretion time-scale if it is to be replaced by a sink,

$$\tau_{\text{ff},i} < \frac{|\mathbf{r}_{ij}|}{\mathbf{r}_{ij} \cdot \mathbf{v}_{ij}}, \quad (4)$$

$$\rho_i > \frac{3\pi}{32G} \left(\frac{\mathbf{r}_{ij} \cdot \mathbf{v}_{ij}}{|\mathbf{r}_{ij}|} \right)^2. \quad (5)$$

Our simulations have been tested with sink creation densities ranging from 10^{-12} to $10^{-17} \text{ g cm}^{-3}$, and we are confident that a sink creation density of $10^{-15} \text{ g cm}^{-3}$ is well converged.¹

The computational domain is open in the x - and y -directions, but periodic in z , the long axis of the filament (see Wünsch et al. in preparation for the implementation of the modified Ewald field). This allows us to study the fragmentation of an infinitely long filament, and ignore the complicating effects of global longitudinal collapse (Clarke & Whitworth 2015).

To generate the initial conditions, a cylindrical settled glass of particles with uniform density is stretched so that it reproduces the density profile,

$$\rho(R, z) = \frac{\rho_0 R_0}{R}. \quad (6)$$

Where $R \equiv (x^2 + y^2)^{1/2}$ and ρ_0 is the density at $R_0 = 0.1 \text{ pc}$. Note that this is a uniform density profile in the longitudinal z direction. The initial velocity field is

$$\mathbf{v} = -v_0 \hat{\mathbf{R}} + \mathbf{v}_{\text{TURB}}. \quad (7)$$

The first term of the velocity field is identical to the field used in CWH16, a radially convergent velocity field to model the formation of a filament. The second term is a turbulent velocity field that is added to the gas to seed density perturbations. The characteristics of this turbulent field are discussed in Section 2.1.

Values of $\rho_0 = 150 M_{\odot} \text{ pc}^{-3}$ and $v_0 = 0.75 \text{ km s}^{-1}$ are used, as these are the fiducial values in CWH16; this corresponds to a mass accretion rate on to the filament of $\sim 70 M_{\odot} \text{ pc}^{-1} \text{ Myr}^{-1}$, consistent with accretion rates inferred observationally (Kirk et al. 2013; Palmeirim et al. 2013).

The turbulent cylinder of particles has a radius of $r_{\text{MAX}} = 1 \text{ pc}$ and a length of $L = 3 \text{ pc}$. This provides a sufficiently large computational domain to allow us to study a wide range of possible perturbation wavelengths, while maintaining good resolution.

Artificial viscosity is needed to capture shocks, but it is known to overly dampen motions on the order of the smoothing length. Therefore, the simulations use the time-dependent artificial viscosity described in Morris & Monaghan (1997) to lessen this effect.

After the first sink particle forms, the simulations run until the sinks have accreted roughly 10 per cent of the initial gas mass. After this time, feedback mechanisms such as protostellar jets are expected to play an important role, and, as these processes are not modelled, the simulations are terminated.

The simulations are run with 450 000 particles; each SPH particle has a mass of $6.3 \times 10^{-4} M_{\odot}$, resulting in a conservative mass resolution of $6.3 \times 10^{-2} M_{\odot}$. Tests with different numbers of particles show that the simulations are converged.²

2.1 Turbulent velocity fields

The initial turbulent velocity field, \mathbf{v}_{TURB} , is generated using the procedure described in Lomax, Whitworth & Hubber (2015). The turbulent velocity field is defined by a power spectrum, $P(k) \propto k^{-\alpha}$, where k is the velocity mode's wavenumber. Burgers turbulence, $\alpha = 4$, is appropriate for highly supersonic turbulence, while $\alpha = 11/3$, known as Kolmogorov turbulence, is appropriate for subsonic turbulence in an incompressible fluid [see Federrath (2013)

¹ For an overview of the standard sink creation criteria and a convergence test showing the implementation of the new criteria, see Appendix A.

² The results of these simulations are presented in Appendix B.

for a discussion of the difference between Burgers and Kolmogorov spectra.]

For a compressible fluid with transonic turbulence, the exponent is expected to lie between these two values. In both the Burgers and Kolmogorov cases, the majority of the power lies in the small wavenumber, large wavelength modes and so the exact choice of exponent is not very significant. This is shown to be the case when the exponent is greater than 3 in prestellar core simulations presented by Walch, Whitworth & Girichidis (2012). For this work, we use $\alpha = 4$.

We do not include the longest wavelength modes in the x and y directions, $\mathbf{k} = (1, 0, 0)$ and $(0, 1, 0)$, as the first term of equation (7) can be considered as an imposed velocity mode in those directions.

We consider the effect that the ratio of compressive to solenoidal kinetic energy has on filament fragmentation. Purely compressive turbulence is defined as a curl-free velocity field and purely solenoidal turbulence is defined as a divergence-free velocity field. The distinction between these types of turbulent fields, and their effects on star formation, has been explored in many papers (e.g. Federrath, Klessen & Schmidt 2008; Federrath et al. 2010b; Federrath & Klessen 2012).

A velocity field with a user-defined ratio of compressive to solenoidal kinetic energy can be constructed using Helmholtz’s theorem [see section 2.1.3 of Lomax et al. (2015) for more details]. We consider two cases, purely compressive and a ‘natural’ mix, i.e. where the solenoidal modes have twice the power of the compressive modes. In the nomenclature used by Lomax et al. (2015), these two cases correspond to $\delta_{\text{sol}} = 0$ and $\delta_{\text{sol}} = 2/3$ respectively.

A turbulent field is defined by its power spectrum, which determines the distribution of energy as a function of wavenumber, and the three dimensional velocity dispersion, $\sigma_{3\text{D}}$, which determines the total amount of energy in the velocity field. We consider three cases, $\sigma_{3\text{D}} = 0.1, 0.4, 1.0 \text{ km s}^{-1}$, which correspond to Mach numbers of $\mathcal{M} \sim 0.25, 1, 2.5$ respectively.

Each turbulent field is generated using a random number seed, and we have performed 10 realizations of each pair of parameters, δ_{sol} and $\sigma_{3\text{D}}$, resulting in a total of 60 simulations.

3 RESULTS

The turbulent field produces density perturbations on many different length scales within the filament (for one example, see Fig. 1). In all simulations, the filament is sub-critical during early times and has a typical width of $\sim 0.1 \text{ pc}$. Gas continues to accrete on to the filament, until it reaches the critical line-density and the regions of high density, formed due to the turbulent velocity field, collapse to form sink particles.

To study the fragmentation of a filament, we work out the sink separation at the end of the simulation when 10 percent of the mass is in sink particles. For each pair of parameters, δ_{sol} and $\sigma_{3\text{D}}$, we work out the sink separations for all 10 realizations to produce a separation distribution. All separations that are below 0.02 pc are removed; this is because we wish to study filament fragmentation into cores, and separations below $\sim 4000 \text{ au}$ are clearly due to core fragmentation resulting in multiple systems. Fig. 2 shows the histograms of the separation distributions for the natural-mix turbulence, $\delta_{\text{sol}} = 2/3$, and Fig. 3 shows the same information for the purely compressive turbulence, $\delta_{\text{sol}} = 0$. The information from each of the 60 simulations is summarized in a set of tables found in Appendix C.

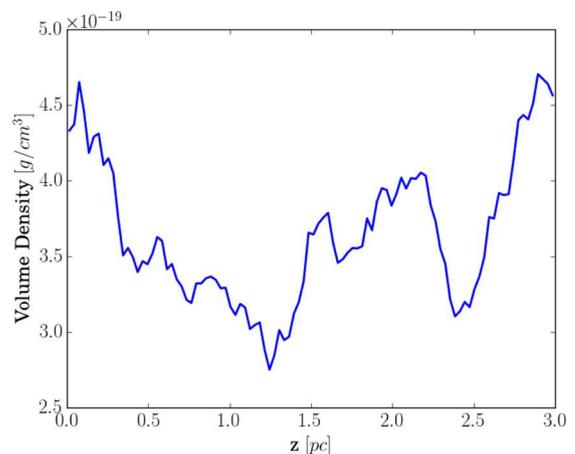


Figure 1. The volume density profile along the z -axis at $t = 0.4 \text{ Myr}$ showing density perturbations on many different scales. In this case, the turbulent field has a natural mix of compressive and solenoidal modes, $\delta_{\text{sol}} = 2/3$, and a subsonic velocity dispersion, $\sigma_{3\text{D}} = 0.1 \text{ km s}^{-1}$.

All six histograms seen in Figs 2 and 3 show a more complicated distribution than that found in CWH16 (their fig. 8); turbulence has thus altered the fragmentation of the filaments considerably.

For the subsonic case (Figs 2a and 3a), the distributions from the natural-mix and purely compressive turbulence share the same morphology. Both core separation distributions show two peaks at the same locations, one at $\sim 0.1 \text{ pc}$ and the other at $\sim 0.5 \text{ pc}$. The small insets show the small-scale separations, $< 0.3 \text{ pc}$, in more detail for both values of δ_{sol} . Here one can see that there is a small difference in the two distributions, the natural mix produces a peak just above 0.1 pc , while the purely compressive turbulence produces a peak just below 0.1 pc .

The transonic case (Figs 2b and 3b) is more complicated. The natural-mix turbulence has a wide range of core separations and a peak at $\sim 1 \text{ pc}$. The purely compressive turbulence produces a bimodal distribution with peaks at ~ 0.5 and $\sim 1.2 \text{ pc}$.

The supersonic case (Figs 2c and 3c) produces two very different distributions. The natural-mix turbulence causes a number of filaments to only form one core (the large peak in core separations at 3 pc), those that do fragment into numerous cores do so with a wide range of separation distances with a peak $\sim 1.2 \text{ pc}$. More filaments fragment into multiple cores when the turbulence is purely compressive, and those that do, do so with a bimodal distribution with peaks at ~ 1.5 and $\sim 0.1 \text{ pc}$.

4 DISCUSSION

The nature of the turbulence plays an important role in the fragmentation of a filament when the turbulence is transonic or supersonic. Compressive turbulence produces narrower and more clearly defined core separation distributions, and so is more likely to lead to quasi-periodically fragmented filaments. Natural turbulence produces wider distributions with less well defined peaks.

4.1 Initially subsonic turbulence

For subsonic turbulence, the nature of the turbulence does not play a significant role in the fragmentation. This can easily be understood by considering the fact that the ratio of initial gravitational potential energy over initial turbulent energy for these simulations is ~ 100 , thus the dynamics are dominated by gravity.

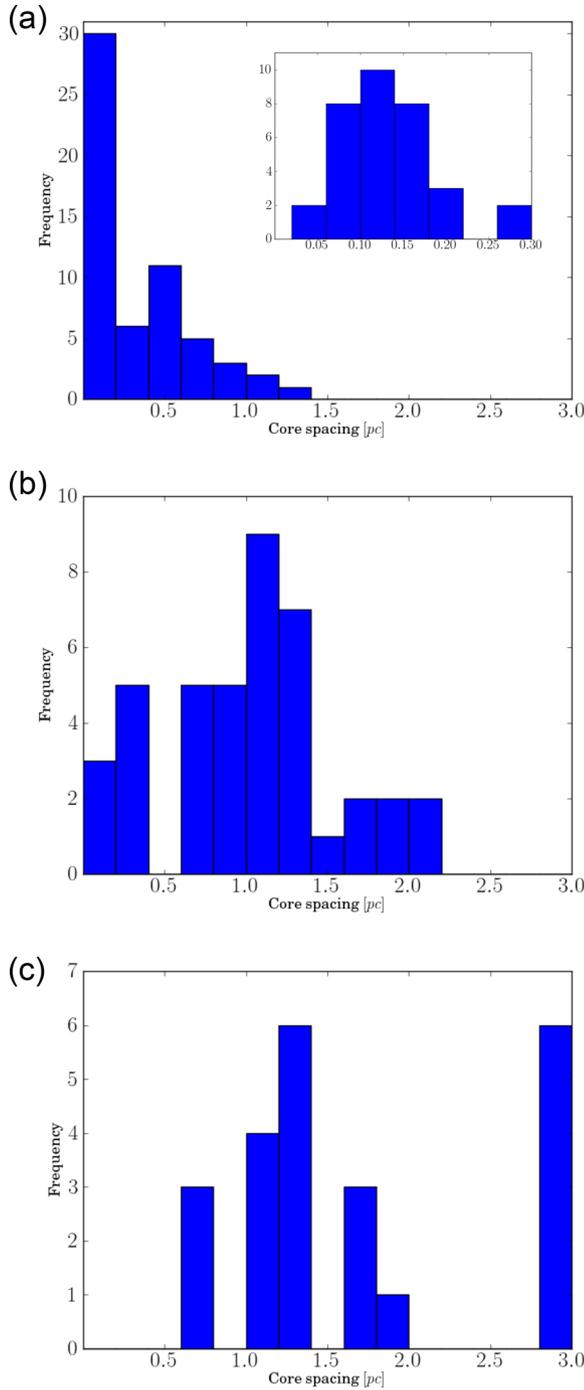


Figure 2. Histograms showing the distribution of core separation distances for the set of simulations initialized with a natural mix of turbulence, $\delta_{\text{sol}} = 2/3$, for (a) $\sigma_{3\text{D}} = 0.1 \text{ km s}^{-1}$, (b) $\sigma_{3\text{D}} = 0.4 \text{ km s}^{-1}$ and (c) $\sigma_{3\text{D}} = 1 \text{ km s}^{-1}$. Parts a, b and c have 58, 41 and 23 separations respectively. The sub-sonic case (a) has an inset to show the distribution of small-scale separations ($<0.3 \text{ pc}$) in more detail. Note that a separation of 3 pc is recorded when the filament has only produced one core, since this is the length of the computational domain and hence the length of the filament.

Both types of turbulence show bimodal distributions, neither peak corresponding to that suggested by the most unstable mode of a filament, given by equation (1). Taking $a_0 = 0.37 \text{ km s}^{-1}$ and $\tau_{\text{CRIT}} = 0.45 \text{ Myr}$, one would expect to see a peak at $\sim 0.3 \text{ pc}$. These are the values for the fiducial case in CWH16, which

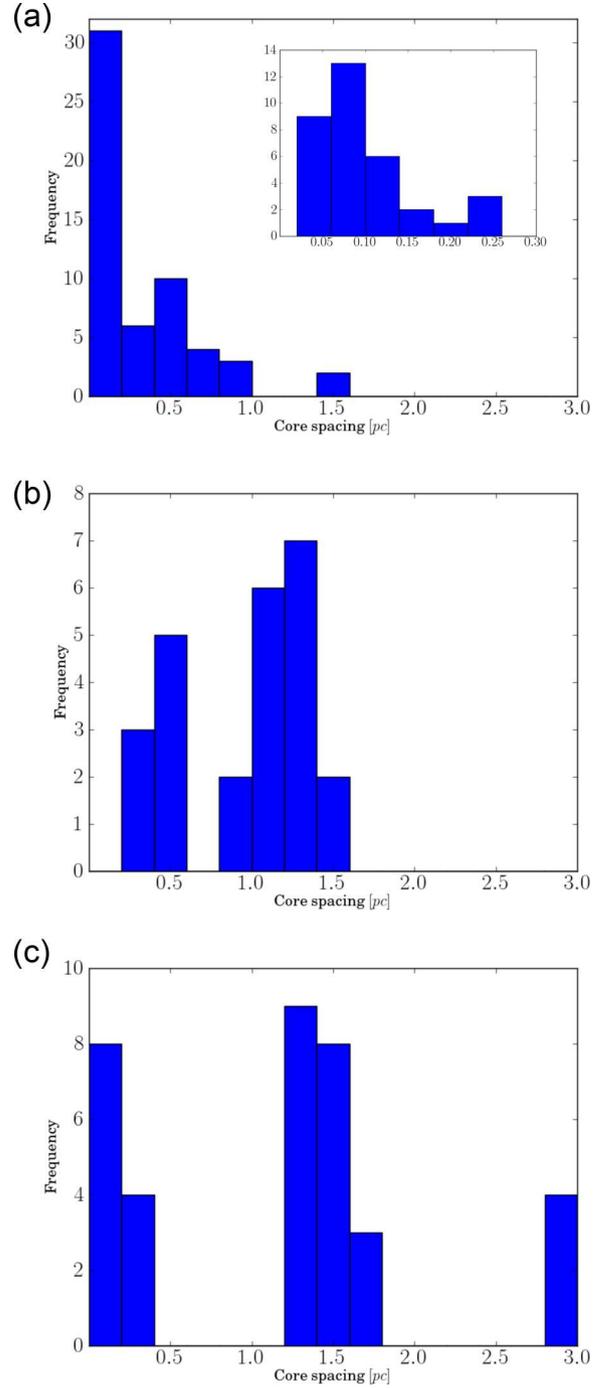


Figure 3. Histograms showing the distribution of core separation distances for the set of simulations initialized with purely compressive turbulence, $\delta_{\text{sol}} = 0$, for (a) $\sigma_{3\text{D}} = 0.1 \text{ km s}^{-1}$, (b) $\sigma_{3\text{D}} = 0.4 \text{ km s}^{-1}$ and (c) $\sigma_{3\text{D}} = 1 \text{ km s}^{-1}$. Parts a, b and c have 56, 25 and 36 separations respectively. The sub-sonic case (a) has an inset to show the distribution of small-scale separations ($<0.3 \text{ pc}$) in more detail. Note that a separation of 3 pc is recorded when the filament has only produced one core, since this is the length of the computational domain and hence the length of the filament.

share the same accretion rate and temperature as the simulations presented here.

However, equation (1) uses the isothermal sound speed that is likely to be inappropriate in a turbulent environment. In the presence of turbulence, one ought to use the effective sound speed defined

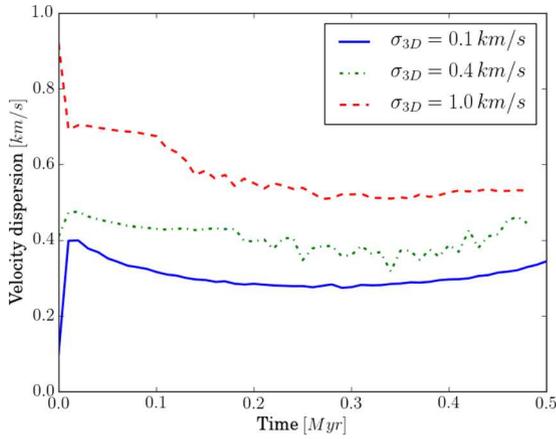


Figure 4. Average velocity dispersion as a function of time for the subsonic (solid blue), transonic (dot-dashed green) and supersonic (dashed red) for natural-mix turbulence simulations. In all three cases, the velocity dispersion tends to stabilize at a roughly transonic level, $\sim 0.4 \pm 0.15 \text{ km s}^{-1}$.

as $a_{\text{EFF}} = \sqrt{a_o^2 + \sigma_{1D}^2}$, where σ_{1D} is the one-dimensional velocity dispersion. For isotropic turbulence, $\sigma_{1D} = \sigma_{3D}/\sqrt{3}$, where σ_{3D} is the three-dimensional velocity dispersion. Changing a_o for a_{EFF} in equation (1), the most unstable mode in a turbulent filament is given by

$$\lambda_{\text{DOM}} \sim 2\tau_{\text{CRIT}} a_{\text{EFF}}. \quad (8)$$

To calculate the three-dimensional velocity dispersion within a filament, one must first define the edge of the filament. This is done by finding the azimuthally and longitudinally averaged radial profile of the filament and determining the radius at which the density profile blends into the background profile; for these simulations that is the radius where $\rho \propto r^{-1}$, the initial accretion flow's density profile given by equation (6). All SPH particles that lie within this bounding radius are considered to be part of the filament. The three-dimensional velocity dispersion is calculated using velocities in the cylindrical coordinate system, (r, θ, z) ; this is done to avoid artificially high velocity dispersions when one uses Cartesian coordinates. At each time-step, we find the average three-dimensional velocity dispersion of the 10 realizations for each parameter pair. The resulting velocity dispersions for the natural-mix turbulence simulations are shown in Fig. 4. One sees that, no matter what the initial turbulent velocity dispersion is, the three-dimensional velocity dispersion within the filament tends to approximately the same transonic value, $\sim 0.4 \pm 0.15 \text{ km s}^{-1}$. The velocity dispersion rises after 0.5 Myr as the filament begins to fragment. This corroborates the results of Federrath (2016) who also find transonic velocity dispersion in filaments using different initial conditions and a different numerical method.

Taking a value of 0.4 km s^{-1} for σ_{3D} , the effective sound speed in these filaments is $a_{\text{EFF}} \sim 0.45 \text{ km s}^{-1}$. Radial collapse begins at $\tau_{\text{CRIT}} \sim 0.5 \text{ Myr}$. Thus the most unstable mode given by equation (8) is $\sim 0.45 \text{ pc}$, consistent with the large-scale peak in the core separation distributions for the initially subsonic filaments.

The small-scale peak at $\sim 0.1 \text{ pc}$ is consistent with the effective Jeans length given by $a_{\text{EFF}}/\sqrt{G\rho}$, where ρ is the average density in the filament and G is the gravitational constant. The average density in these filaments is of the order of 10^{-19} to $10^{-18} \text{ g cm}^{-3}$, which results in a Jeans length of $0.05\text{--}0.17 \text{ pc}$.

If the large-scale separation is regulated by a variant of the dispersion relation found by CWH16, it may be used to determine

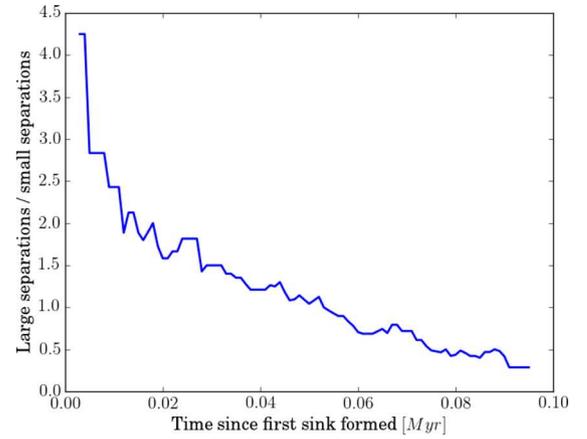


Figure 5. Ratio of the number of large-scale core separations ($>0.3 \text{ pc}$) over the number of small-scale core separations ($<0.3 \text{ pc}$) as a function of time for subsonic natural-mix turbulence simulations. Large-scale separations dominate at early times, but small-scale separations become more common very quickly, on the order of a tenth of a megayear.

the age and mean accretion rate of a filament. One needs to substitute the effective sound speed for the isothermal sound speed in equations (2) and (3) resulting in,

$$\tau_{\text{AGE}} \geq \tau_{\text{CRIT}} \simeq \frac{\lambda_{\text{CORE}}}{2a_{\text{EFF}}}, \quad (9)$$

and

$$\langle \mu \rangle \simeq \frac{2a_{\text{EFF}}\mu}{\lambda_{\text{CORE}}}. \quad (10)$$

Filaments assembled from gas with subsonic turbulence, or where gravity dominates over turbulence, therefore possess two preferential fragmentation length scales: a large fragmentation length scale that is consistent with a modified version of the filamentary fragmentation model presented in CWH16 and a small fragmentation length scale that is consistent with the effective Jeans length in these filaments.

It is important to note how these fragmentation length scales evolve. Fig. 5 shows the number of large-scale core separations ($>0.3 \text{ pc}$) divided by the number of small-scale core separations ($<0.3 \text{ pc}$) as a function of time since the first sink particle forms. Large-scale fragmentation proceeds first but is quickly followed by small-scale fragmentation such that 0.1 Myr after fragmentation begins, there are roughly twice as many small length scale core separations as large length scale core separations. The rapid increase in small-scale Jeans length separations after collapse begins reduces the periodicity of the fragmentation. The fact that the phase of a filament's life when it is dominated by periodic fragmentation is short lived may explain why quasi-periodically fragmented filaments are rare, despite both equilibrium and non-equilibrium models suggesting they ought to be standard.

Thus, initially subsonic filaments, or those where gravity dominates over turbulence, fragment in a two-tier hierarchical fashion, where large-scale fragmentation occurs first on a length scale determined by filamentary fragmentation and then those structures proceed to fragment on a smaller scale determined by the effective Jeans length. This type of hierarchical multitiered fragmentation has recently been observed in the Orion Integral Shaped Filament (Kainulainen et al. 2016b; Teixeira et al. 2016).

4.2 Initially transonic turbulence

When the turbulence in the accretion flow is subsonic, the separation of fragments is largely determined by gravitational fragmentation – as described in the preceding subsection. However, once the turbulence in the accretion flow is transonic, the separation of fragments is largely determined by the dominant wavelengths in the turbulence. Specifically, since most of the turbulent energy is in the longer wavelength modes, there is a clustering of separations in the range 1.0–1.5 pc, corresponding to the modes with $k_z = 2-3$ (recall that the box is 3 pc long). This trend is independent of whether the turbulence comprises purely compressive modes, or a natural mix of compressive and solenoidal modes.

As the fragmentation is dominated by the turbulent field, the exact position of the peak in core separations is likely to be the consequence of our choice of λ_{MAX} , the maximum wavelength in the turbulent field, and is a numerical effect. If λ_{MAX} were reduced, the position of the peak would likely move to a lower value. This effect has been studied in detail for the case of a turbulent pre-stellar core by Walch et al. (2012).

As well as the ‘turbulent’ peak at ~ 1.2 pc, the purely compressive turbulence simulations also show a peak at ~ 0.5 pc, which is consistent with gravitational filamentary fragmentation (equation 8); this peak is not apparent in the natural-mix turbulence. This suggests that the case of purely compressive turbulence is better described by the gravitational fragmentation model (modified by combining the thermal and turbulent contributions to the velocity dispersion) than the case of natural-mix turbulence, which contains solenoidal modes. The purely compressive case is thus more likely to produce quasi-periodically fragmented filaments.

4.3 Initially supersonic turbulence

The initially supersonic cases also show a marked difference due to the nature of the turbulence. This is expected when one considers the fact that the initial turbulent energy is roughly equal to the initial gravitational potential energy, thus the dynamics are markedly influenced by the turbulence.

Both supersonic cases show the clustering of core separations around ~ 1.5 pc due to the turbulent field dominating the fragmentation process. The compressive turbulence produces the narrower of the two distributions, as in the transonic case. There is a peak at very small separations in the purely compressive case which is not apparent in the natural-mix case. This is predominately composed of separations in the range 0.02–0.05 pc, i.e. just above the cut-off imposed to remove multiples. It is therefore likely that this peak is due to a number of wide multiples that just exceed the cut-off, and we do not consider these separations further.

A natural mix of modes tends to dampen fragmentation globally, leading to a large number of filaments that only produce one core. Natural-mix turbulence delays the onset of collapse, $\bar{t}_{\text{sink}} = 0.717$ Myr, more than purely compressive turbulence, $\bar{t}_{\text{sink}} = 0.611$ Myr. However, the time then taken for 10 per cent of gas to convert into sinks is 0.131 Myr for the natural mix and 0.128 Myr for the purely compressive turbulence. Solenoidal modes therefore act as a support on large scales, but are unable to slow star formation once it has started. This is different to the results seen in molecular cloud simulations (e.g. Federrath & Klessen 2012) that show that if turbulence is allowed to decay, it strongly reduces the effect of the mixture of turbulent modes.

The increase in initial turbulence also produces a significant change in the morphology of the filaments. This can be seen in

column density maps of both the natural-mix and the purely compressive cases, which show a number of elongated sub-structures (Fig. 6). The elongated structures seen in the column density maps are real continuous structures in volume density and may be similar to the fibres recently seen in Taurus (Hacar et al. 2013; Tafalla & Hacar 2015). A large number of these elongated structures are seen to overlap and merge to form hub-like features, in which most of the cores form; this is somewhat different from the fibres seen in Taurus, which appear to fragment independently of each other.

The presence of fibre-like structures may explain why the supersonic cases produce a markedly different core separation distribution from the sub- and transonic simulations, which do not form such structures. In the supersonic cases, the fibre-like structures dominate the fragmentation process.

An important point to make is that the fibres identified observationally are found as velocity-coherent structures in position–position–velocity (PPV) space while these elongated structures are seen in position–position (PP) space in column density, and in position–position–position (PPP) space in volume density. Without synthetic images it is impossible to make a direct comparison between the fibre-like structures seen in these simulations and the fibres observed. None the less one can consider how the fibre-like structures appear in three dimensions. Fig. 7 shows a slice at $y = 0$ pc with the gas velocity in the y -direction, the ‘line-of-sight’ velocity, and volume density contours overlaid for one of the natural-mix initially supersonic simulations at $t = 0.5$ Myr, the time at which the filament becomes globally thermally supercritical. The density contours are at 2, 4, 6, 8, $10 \times 10^{-20} \text{ g cm}^{-3}$. One can see that the velocity in the elongated structures varies smoothly and by small amounts. The regions that exhibit large velocity differences are either outside the contours, and so are diffuse, or associated with compact high density areas that are locally collapsing. Thus, although one cannot be certain that an observer would identify these elongated sub-structures as fibres, they are velocity coherent and continuous in volume density.

4.4 Dendrograms

To investigate quantitatively how hierarchical and sub-structured these filaments are, one may use dendrograms (Rosolowsky et al. 2008). Here we use the PYTHON package ASTRODENDRO.³ Dendrograms are constructed from three-dimensional volume density cubes with a resolution of 0.01 pc at $t = 0.5$ Myr, the time at which the filaments become roughly thermally supercritical. The dendrograms are constructed using the parameters: `min_value` = $10^{-20} \text{ g cm}^{-3}$, the lowest density that a data point must have to be considered when building the dendrogram; `min_delta` = $5 \times 10^{-21} \text{ g cm}^{-3}$, the minimum density contrast between a leaf and its branch; and `min_npix` = 100, the minimum number of pixels needed for a leaf to be considered a true structure, corresponding to a sphere with a radius ~ 0.03 pc. Fig. 8 shows two example dendrograms, one from a natural-mix turbulence simulation and the other from a purely compressive turbulence simulation.

One can obtain two statistics from the dendrograms that quantify the amount of sub-structure and how hierarchical that sub-structure is. The number of leaves in a dendrogram, N_{leaf} , tells one how fragmented a structure is, the more leaves the more fragments are present. The number of levels, N_{level} , from the highest leaf, that is the leaf that has the largest number of branches between it and the

³ <http://www.dendrograms.org>

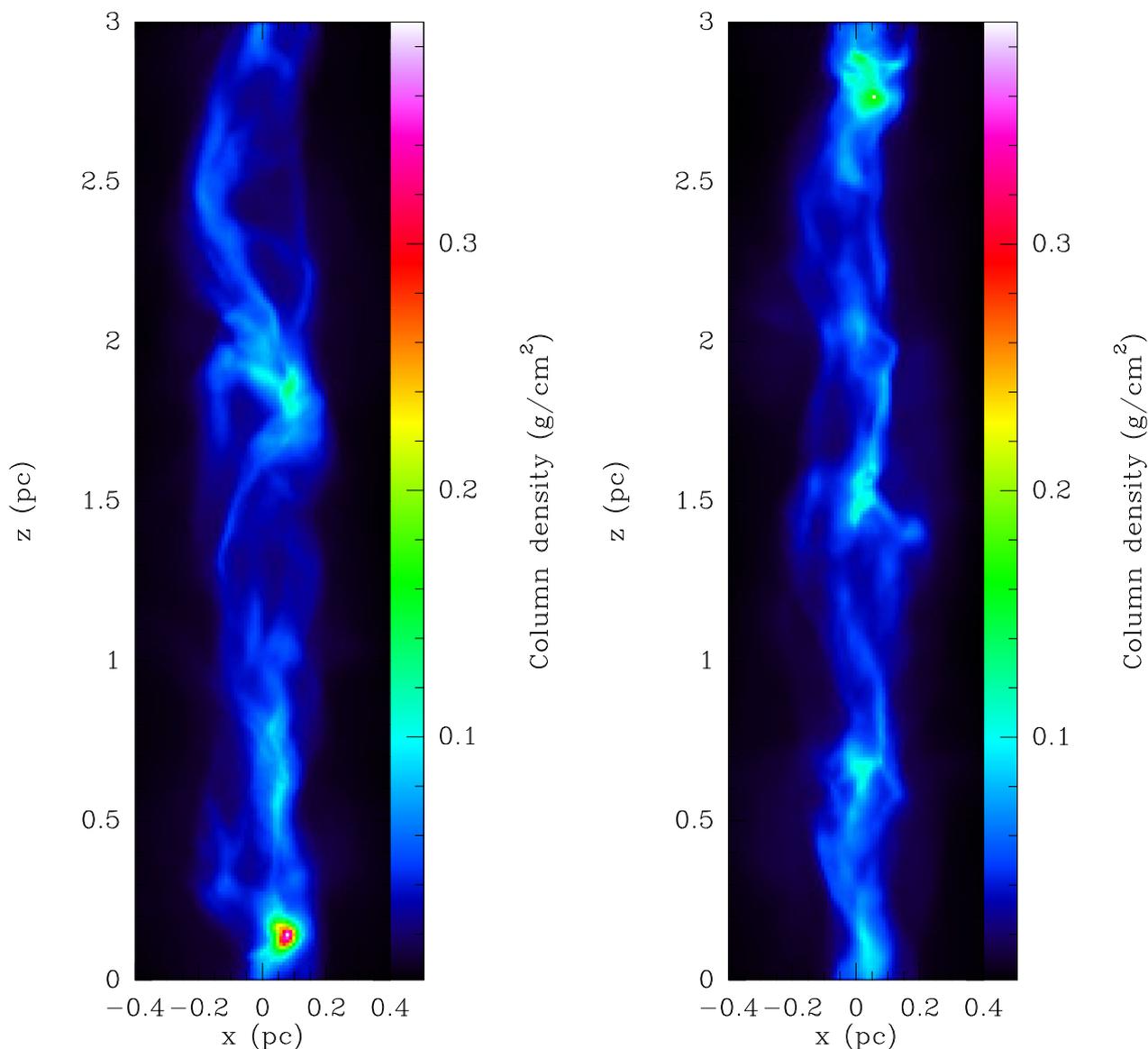


Figure 6. Column density maps at $t = 0.5$ Myr for two of the filaments with initially supersonic turbulence, $\sigma_{3D} = 1 \text{ km s}^{-1}$ but different types of turbulence. On the left, (a), is the natural-mix case, $\delta_{\text{sol}} = 2/3$. On the right, (b), is the purely compressive turbulence, $\delta_{\text{sol}} = 0$. In both cases, we see numerous elongated substructures.

trunk of the dendrogram, tells one how hierarchical the structure is; the more levels, the more nested the sub-structure is. A natural mix of turbulent modes produces both a more fragmented and a more hierarchical structure than the purely compressive turbulence; the mean values and their associated errors: $N_{\text{leaf}} = 31.7 \pm 1.6$ and $N_{\text{level}} = 20.9 \pm 1.5$ for the natural-mix case, and $N_{\text{leaf}} = 22.5 \pm 1.8$ and $N_{\text{level}} = 14.3 \pm 1.1$ for the purely compressive case. Though the exact values of N_{leaf} and N_{level} change when different values for min_value , min_delta and min_npix are used to construct the dendrograms, the result that the natural-mix turbulence is more fragmented and hierarchical does not change. One can see this difference in sub-structure in Fig. 8.

As an observer does not have access to the three-dimensional volume density structure of a filament, but instead must use the two-dimensional column density, we produce dendrograms using the column density of the simulations. The dendrograms are constructed using: $\text{min_value} = 3 \times 10^{-4} \text{ g cm}^{-2}$, $\text{min_delta} =$

$1.5 \times 10^{-4} \text{ g cm}^{-2}$ and $\text{min_npix} = 21$. These values for min_value and min_delta are chosen as they are the choices we made for the three-dimensional volume density dendrograms multiplied by 0.01 pc, the grid resolution. The choice of min_npix was made as it is $100^{2/3}$, the two-dimensional equivalent of our three-dimensional choice. The two cases, natural-mix turbulence and purely compressive turbulence, are indistinguishable from each other when one uses their column density dendrograms: $N_{\text{leaf}} = 15.8 \pm 0.7$ and $N_{\text{level}} = 9.7 \pm 0.5$ for the natural-mix turbulence, and $N_{\text{leaf}} = 14.4 \pm 0.6$ and $N_{\text{level}} = 8.9 \pm 0.6$ for the purely compressive turbulence. Fig. 9 shows two example dendrograms built using the column density, one constructed from a natural-mix turbulence simulation and the other from a purely compressive turbulence simulation. One can see that there is no significant difference between these dendrograms.

This means that dendrograms derived from column density maps are unable to accurately detect differences in the three-dimensional structure, and that one ought to be cautious when using them to

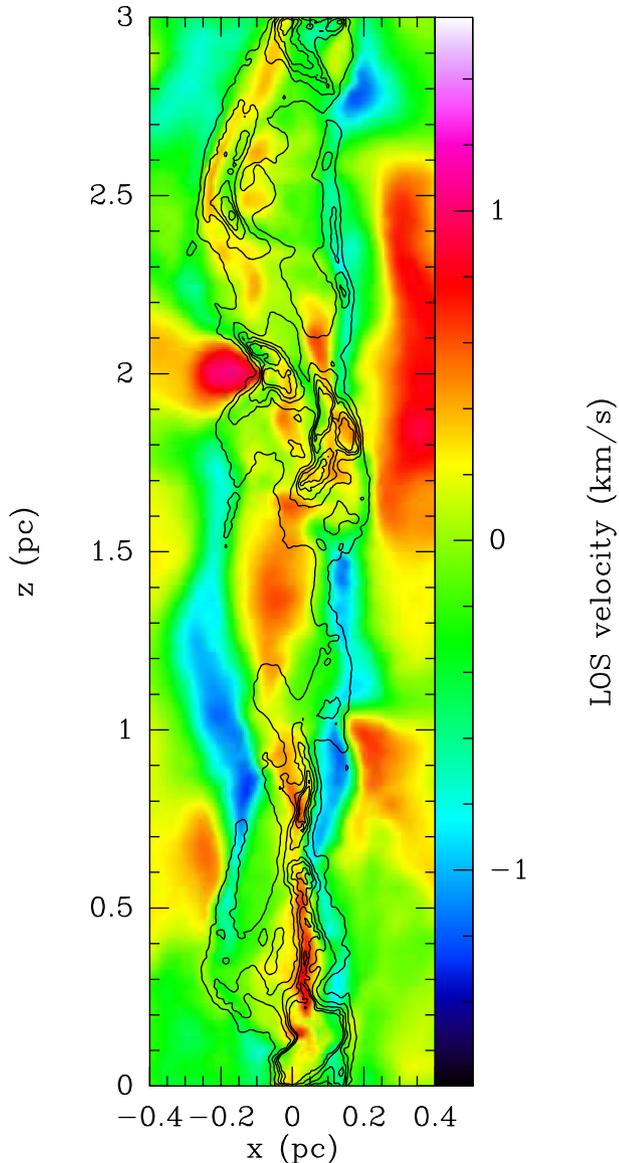


Figure 7. A map of the velocity component perpendicular to the plane, the ‘line-of-sight’ velocity v_y , at $y = 0$ pc with density contours overlaid for an initially supersonic natural-mix turbulence simulation at $t = 0.5$ Myr. The density contours are at 2, 4, 6, 8, 10×10^{-20} g/cm³. One can see that the dense elongated structures exhibit smooth and small variations in velocity. Those regions that show large variations are in the diffuse gas, outside the density contours or in the high density cores that are undergoing collapse.

compare different regions. Perhaps dendrograms constructed using PPV data may show the differences in structure, and this will be investigated in a future paper.

4.5 The formation of fibre-like structures

The formation of the fibre-like structures *in situ* shows that the fray and fragment scenario as proposed by Tafalla & Hacar (2015) is possible. A single main filament first forms due to the colliding flows. As mass is added to the main filament, it fragments to form elongated sub-structures, and eventually some of these fibre-like structures become unstable and fragment into cores. What is more common in these simulations is that hub networks appear and collapse occurs in the hubs. The appearance of hub networks is a small

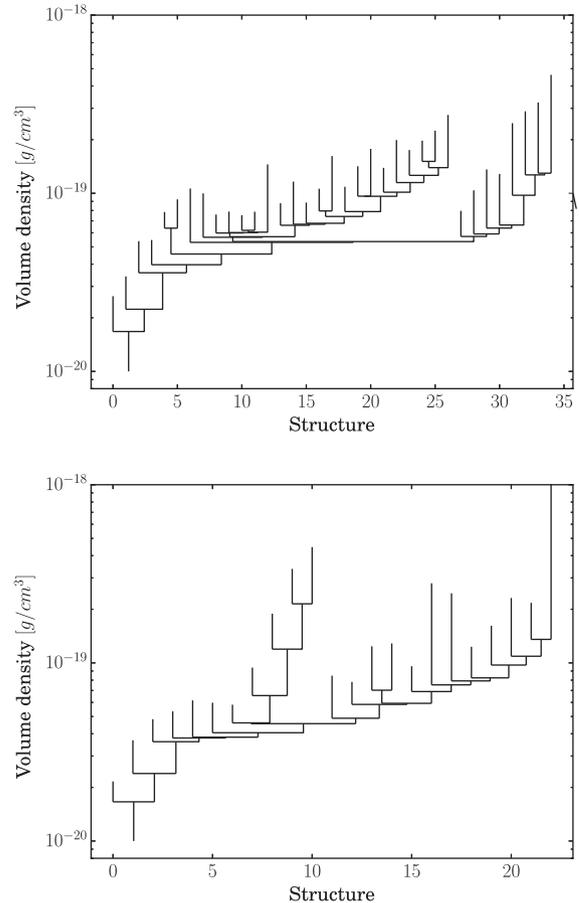


Figure 8. Dendrograms constructed using the three-dimensional volume density cubes of (top) a simulation with a natural mix of turbulence, and (bottom) a simulation with purely compressive turbulence. One can see that a natural mix of turbulence produces greater sub-structure, and that sub-structure is more hierarchical, than the simulation with purely compressive turbulence.

modification to the original scenario proposed by Tafalla & Hacar (2015).

Turbulence is the main driving force by which the filaments fragment into elongated sub-structures. Only the initially supersonic turbulence simulations produce such sub-structures, thus they require a high degree of turbulence to form. Gravity cannot be the dominant mechanism for the formation of these fibre-like structures, since gravitationally induced fragmentation causes collapse in the radial direction and produces the classic ‘beads on a string’ cores.

Tafalla & Hacar (2015) suggest that the fibres they observe are formed due to a combination of vorticity and self-gravity. Vorticity is defined as the curl of the velocity field, $\omega \equiv \nabla \times \mathbf{v}$, and is a measure of the local spinning motion in a fluid.

Fig. 10 shows the normalized distributions of the magnitude of the three vorticity components, ω_x , ω_y and ω_z , for an initially supersonic turbulent filament at $t = 0.5$ Myr. One can see that ω_x and ω_y have near identical magnitude distributions. The vorticity component parallel to the longitudinal axis of the filament, ω_z , has a similar distribution to the other components but with a large tail at high magnitude. This is likely a consequence of the filamentary geometry, accretion in the radial direction will primarily produce motions in the x - y plane and appear as higher values of ω_z .

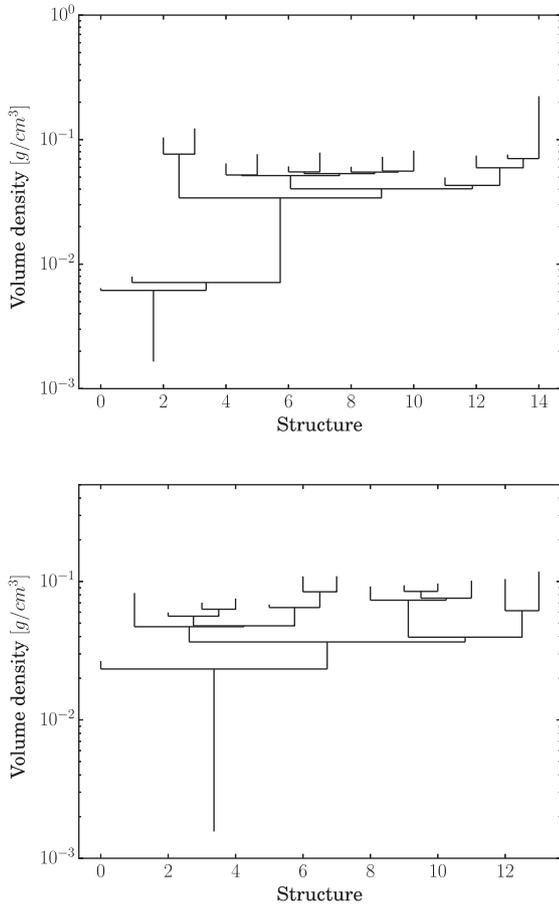


Figure 9. Dendrograms constructed using the two-dimensional column density maps of (top) a simulation with a natural mix of turbulence, and (bottom) a simulation with purely compressive turbulence. One can see that there is not a significant difference in either the amount of sub-structure, or how hierarchical the sub-structure is.

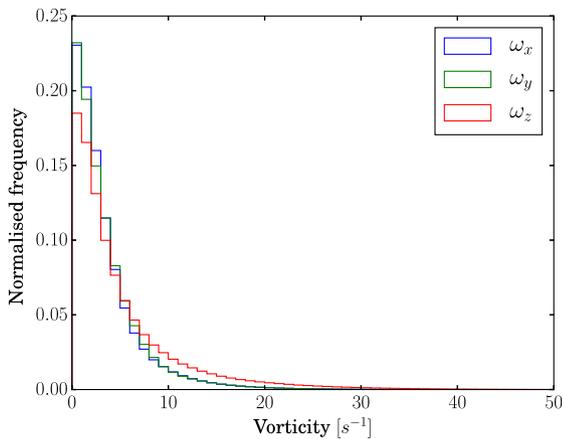


Figure 10. The normalized distributions of the magnitude of the three vorticity components, ω_x , ω_y and ω_z , for an initially supersonic turbulent filament at $t = 0.5$ Myr. The distribution of the vorticity parallel to the longitudinal axis of the filament, ω_z , shows a significant wing at large magnitudes.

Fig. 11 shows a map of the vorticity parallel to the filament’s longitudinal axis, ω_z , at $y = 0$ pc, with volume density contours overlaid, for an initially supersonic turbulent filament at $t = 0.5$ Myr. The density contours are the same as those used in Fig. 7. One can see that a correlation exists between vorticity and density; more precisely the dense elongated structures form in regions in which there exists a large vorticity gradient in the radial direction, $d\omega_z/dx$. Fig. 11 also shows a map of the divergence of the velocity field. The divergence traces the accretion shock on to the main filament but does not appear to correlate with the dense structures. There is also little correlation between the other two components of vorticity, ω_x and ω_y , and density (Fig. 12).

To quantify the correlation between the properties of the velocity field and the density, we perform Spearman rank correlation tests. This gives a non-parametric measure of the correlation between two variables that are connected by a monotonic function. The results can be seen in Table 1. As the direction of rotation is unimportant, the magnitude of the vorticity is used. The magnitude of the vorticity gradient is also used for the same reason. As the number of points considered is very large ($80 \times 80 \times 300$, the number of grid points), the corresponding p -values are vanishingly small, indicating the correlations are statistically significant.

As one expects, the correlation between density and divergence is negative, i.e. dense material has a convergence flow while diffuse material has a divergent flow. However out of the five properties tested, divergence has the weakest correlation with density. Out of the three vorticity components, $|\omega_x|$, $|\omega_y|$, $|\omega_z|$, the vorticity component parallel to the filament’s longitudinal axis, $|\omega_z|$, has the strongest correlation with density, as seen in Figs 11 and 12. Furthermore, the vorticity gradient, defined as $|\delta\omega_z/\delta x|$, shows an even stronger correlation with density, as can be seen in Fig. 11. When the sign of the vorticity and vorticity gradient is considered, Spearman’s ρ is roughly equal to zero, suggesting there is no directional preference. As can be seen in the third column of Table 1, the same trends are apparent when one only considers high density regions, $\rho > 2 \times 10^{-20} \text{ g cm}^{-3}$ i.e. everything within the contours in Figs 11 and 12. The values of Spearman’s ρ are lower, likely due to smaller range over which the correlation is being measured.

When one considers only the magnitude of the divergence, Spearman’s $\rho = 0.30$ is comparable to the correlations between $|\omega_x|$ and $|\omega_y|$, and density. This suggests that the positive correlation between $|\omega_x|$, $|\omega_y|$ and $|\nabla \cdot \mathbf{v}|$, and density, is mainly due to the fact that the velocity field is more rapidly changing in higher density gas. The values of Spearman’s ρ are greater for $|\omega_z|$ and $|\delta\omega_z/\delta x|$, suggesting that the same argument is not capable of explaining the correlation between these quantities and density. It is possible that due to the larger amount of energy in ω_z , as seen in Fig. 10, motions in this direction have a greater impact on structure formation. Thus the stronger correlation is the result of filamentary accretion primarily driving vorticity parallel to the longitudinal axis, leading to fibre-like structures forming.

Fig. 13 shows density plotted against the velocity field properties in Table 1. One can see that a correlation exists between all of these properties and density. Moreover, the relationship between $|\omega_z|$ and $|\delta\omega_z/\delta x|$, and density is both tighter and steeper than the link between the other velocity quantities and density; as expected from the results of the Spearman rank correlation tests.

Fig. 14 is a cartoon illustrating how two nearby sites with antiparallel vorticity vectors will result in a build-up of material and produce sub-structure. The velocity field brings gas parcels in to the centre and forms an area of higher density, gravity can then act to stabilize this structure even though it did not form the structure.

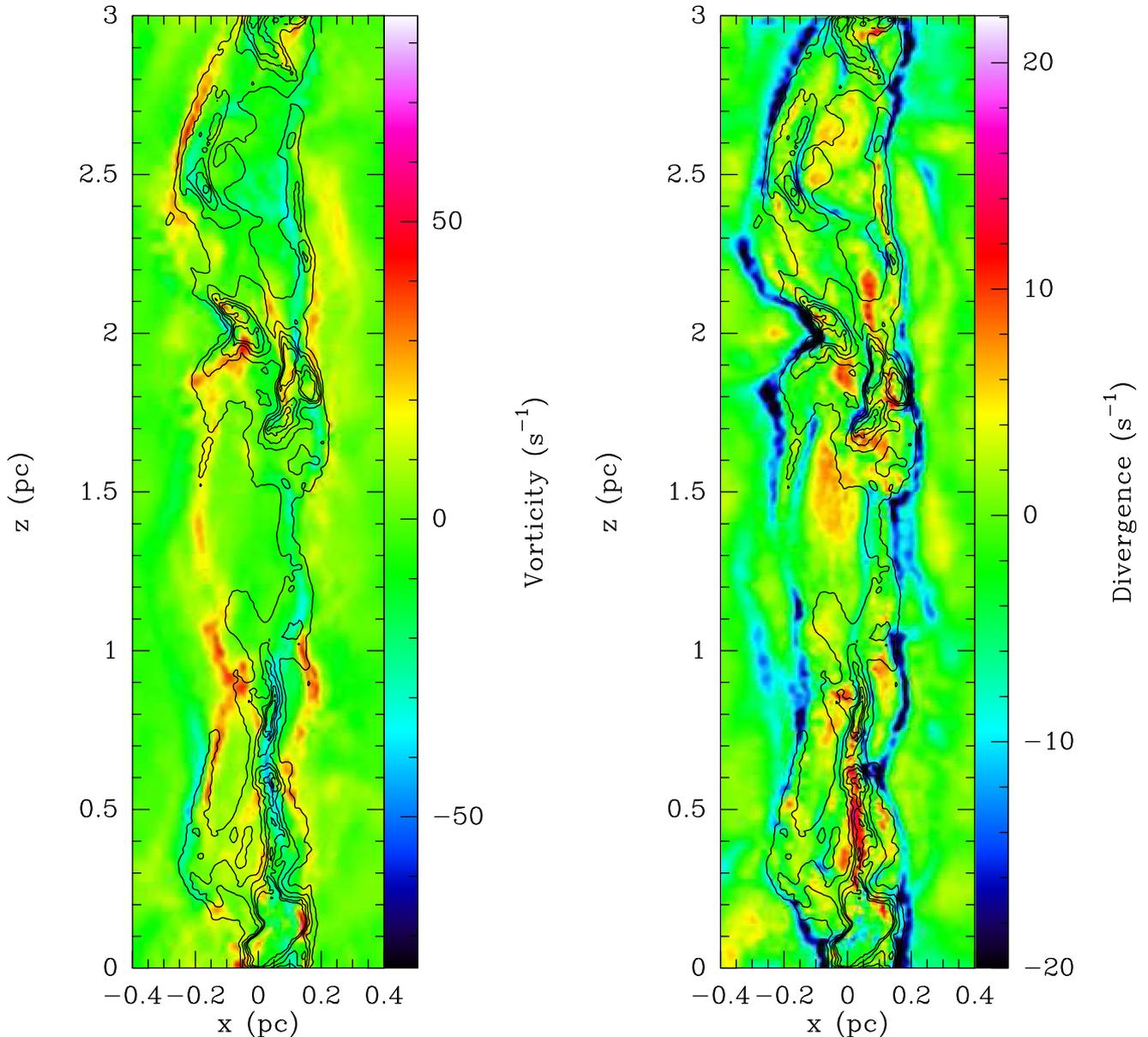


Figure 11. (Left) A map of the vorticity component parallel to the longitudinal axis of the filament, the z -axis, at $y = 0$ pc with density contours overlaid for an initially supersonic natural-mix turbulence simulation. (Right) A map of the divergence of the velocity field in the filament, at $y = 0$ pc with the same density contours. The density contours are at $2, 4, 6, 8, 10 \times 10^{-20} \text{ g/cm}^3$. One can see that the density structures follow the regions in which there exists a large vorticity gradient in the x -direction, i.e. where there are lines of blue and red/yellow next to each other. The divergence is seen to trace the accretion shock on to the main filament, but does not correlate well with the dense structures.

However, even with gravity acting against dispersion, as the fibre-like structures are typically sub-critical, they ought to be short lived. This could explain the prevalence of ‘sterile’ fibres found in Taurus (Hacar et al. 2013; Tafalla & Hacar 2015), which are predominately sub-critical; they are mainly transitory structures created by the filament’s interior velocity field. Only the small proportion of fibres that acquire enough mass to become supercritical before they disperse are ‘fertile’ and fragment to form cores. One would then expect an increase in the number of ‘fertile’ fibres in a more massive and higher density filament, because the velocity field could produce more supercritical fibres before they disperse.

To test that the turbulent velocity field is the dominant cause of the filament fragmenting into fibre-like structures, we re-run a simulation with no self-gravity. Fig. 15 shows the column density

plots of two simulations with the same initial conditions, but one with gravity and the other without. One can see that both simulations show the same general morphology and presence of elongated sub-structure. Gravity has therefore not played a dominant role in forming the fibre-like structures, but does act to hold them together, as seen in Fig. 15(a) where the fibre-like structures are narrower and denser than in the simulation without gravity. This is consistent with the results presented in Federrath (2016), that turbulence is crucial for the structure of filaments but it is gravity that leads to higher peak column densities.

As the filament’s internal turbulence tends to a roughly transonic level no matter what the initial level of turbulence is (as seen in Fig. 4 and discussed in more detail in Section 4.6), the turbulence in the accretion flow must play a role in producing the

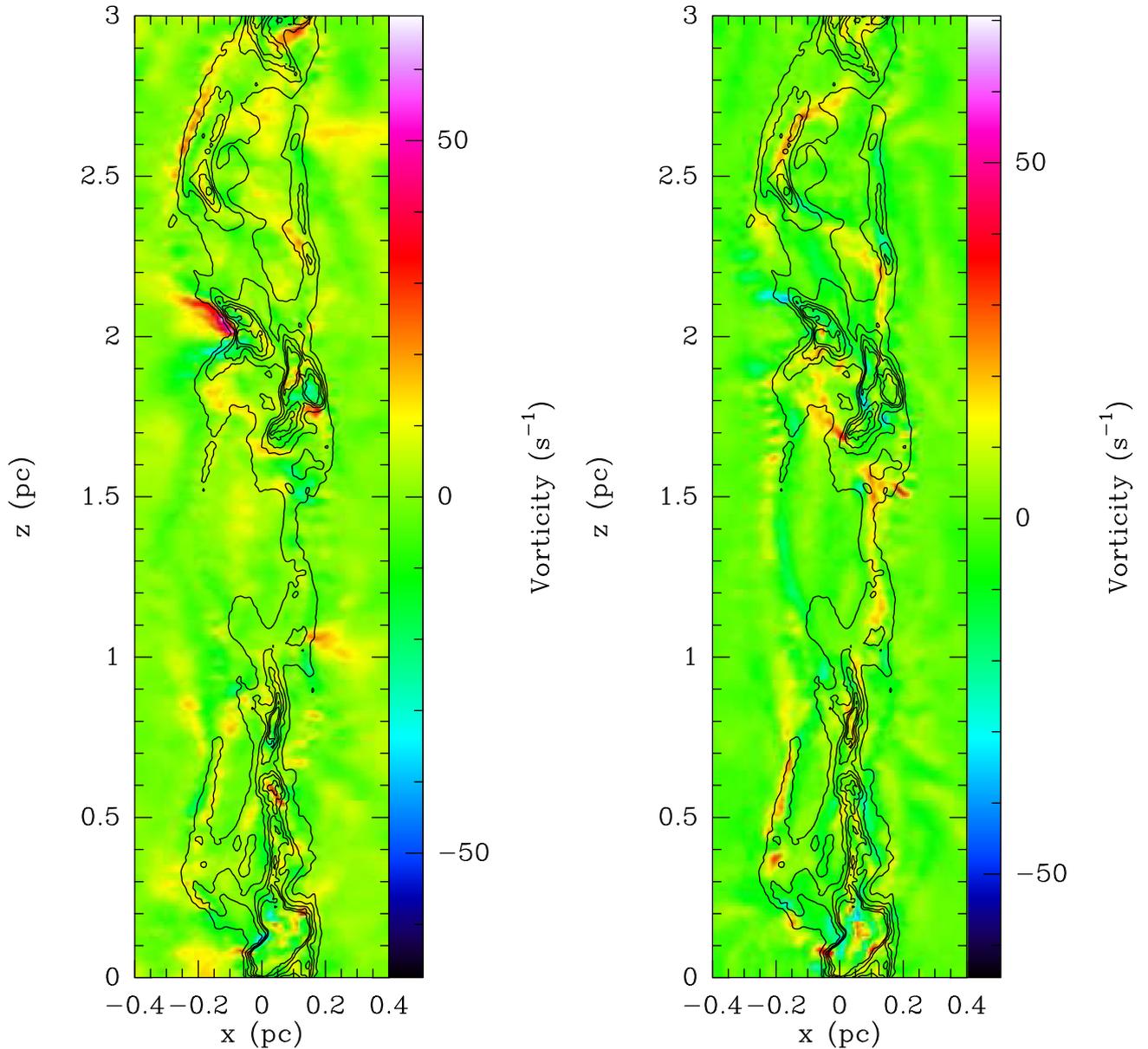


Figure 12. A map of the vorticity component parallel to, on the left, the x -axis and, on the right, the component parallel to the y -axis at $y = 0$ pc with density contours overlaid for an initially supersonic natural-mix turbulence simulation. The density contours are at $2, 4, 6, 8, 10 \times 10^{-20}$ g/cm³. Neither plot shows a strong correlation between vorticity and the density structure.

Table 1. Results of Spearman’s rank correlation tests for the correlation of different spatial derivatives of the velocity field with the volume density.

Velocity quantity	Spearman’s ρ	
	All densities	High densities
Divergence, $\nabla \cdot \mathbf{v}$	-0.16	-0.11
Vorticity, $ \omega_x $	0.31	0.28
Vorticity, $ \omega_y $	0.32	0.30
Vorticity, $ \omega_z $	0.52	0.47
Vorticity gradient, $ \delta\omega_z/\delta x $	0.61	0.58

differences in morphology between simulations with different initial levels of turbulence. Supersonic turbulence in the diffuse accretion flow produces density enhancements that flow on to the main filament. The accretion of this inhomogeneous flow on to the

filament produces vorticity, evidenced by the high vorticity one can see at the boundary of the filament where the accretion shock is located (see Fig. 11). Thus the formation of fibre-like structures is intrinsically linked to a filament’s accretion from a turbulent inhomogeneous medium.

4.6 Accretion driven turbulence

The convergence of the velocity dispersion in all cases to a roughly transonic level is interesting as observers have seen a number of such filaments (Arzoumanian et al. 2013; Hacar et al. 2013; Fernández-López et al. 2014; Kainulainen et al. 2016a). There must exist a continuous mechanism that produces and sustains turbulence in the filaments. Heitsch (2013) propose that accretion flows on to a filament can drive turbulence. They

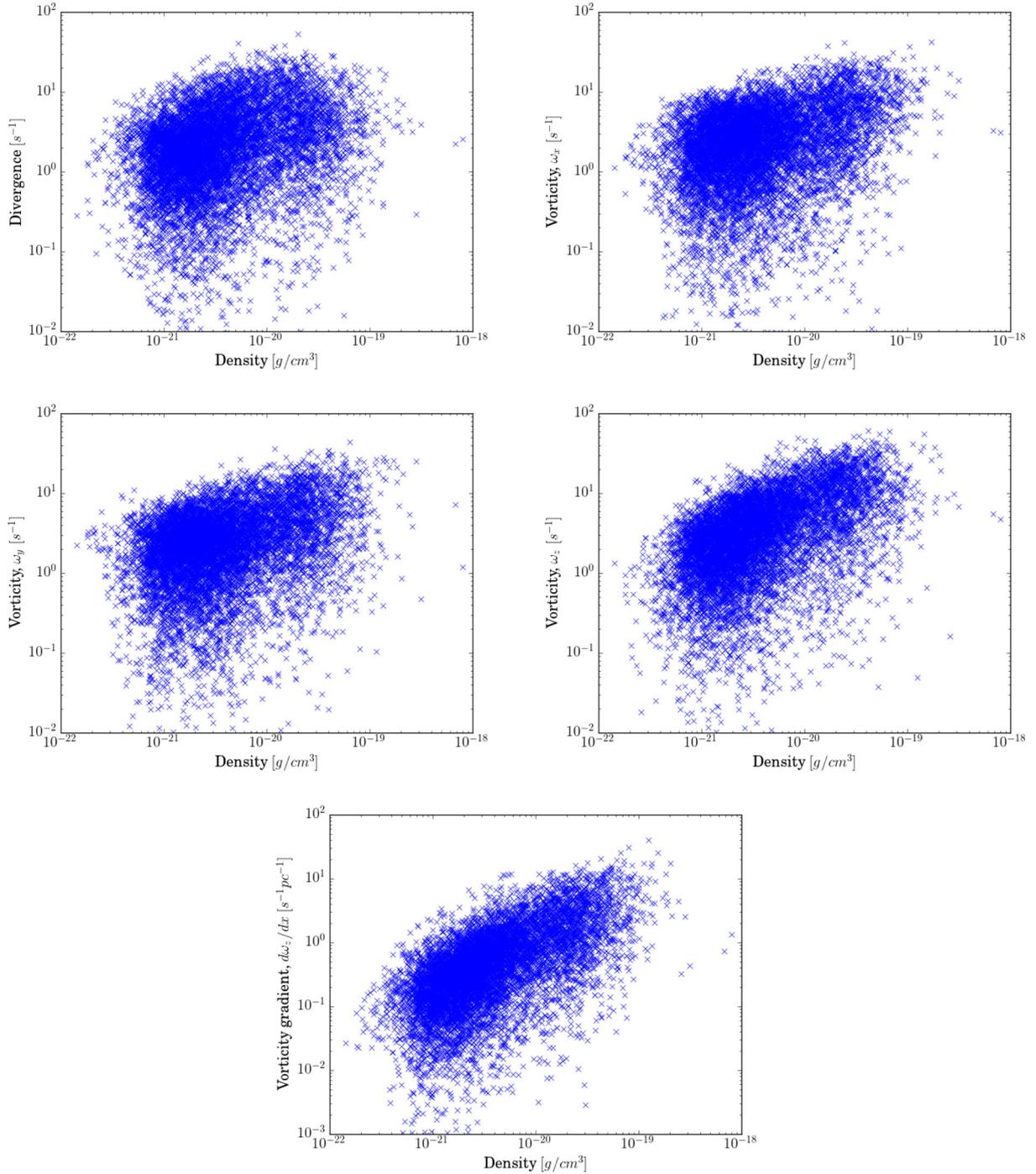


Figure 13. Plots showing volume density against the velocity quantities listed in Table 1. One can see that the relationship between $|\omega_z|$ and $|\delta\omega_z/\delta x|$, and density is both tighter and steeper than the link between the other velocity quantities and density.

conclude that the velocity dispersion driven by accretion is given by,

$$\sigma(t) = \left(2\epsilon R_f v^2(R_f) \frac{\dot{m}(t)}{m(t)} \right)^{1/3}, \quad (11)$$

where ϵ is a driving efficiency factor in the range 0.01–0.1, R_f is the filament’s bounding radius, $v(R_f)$ is the velocity of the accreting gas at the filament’s bounding radius, $m(t)$ is the filament’s line-density at time t and $\dot{m}(t)$ is the accretion rate at time t .

One can use the information from the simulations to find the values of these parameters at every snapshot time and so produce a time evolution of the expected velocity dispersion due to driving. Fig. 16 shows the average expected velocity dispersion due to driving by accretion for $\epsilon = 0.01, 0.05, 0.1$ using the 10 simulations with parameters $\delta_{\text{sol}} = 2/3$ and $\sigma_{3D} = 0.1 \text{ km s}^{-1}$. An efficiency factor in the range of 5–10 per cent is able to drive a velocity dispersion of $\sim 0.4 \text{ km s}^{-1}$; this is true for all six pairs of parameters.

Seifried & Walch (2015) see a similar result in their simulations, the accretion is only able to drive a velocity

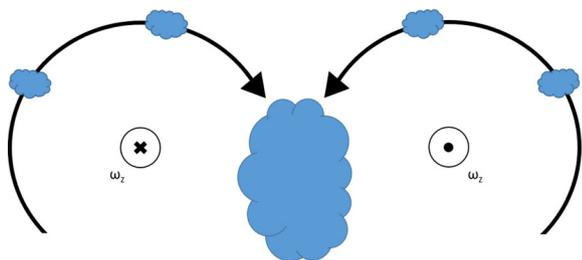


Figure 14. A face down view illustrating how two nearby sites with antiparallel vorticity vectors can produce regions of higher density. The two flows are able to bring gas into the centre from both direction where it can be held together by self-gravity and form a fibre-like structure.

dispersion of at most 0.5 km s^{-1} . The simulations presented in this chapter use a relatively high initial accretion rate on to the filament, $\dot{\mu} = 70 M_{\odot} \text{ pc}^{-1} \text{ Myr}^{-1}$, which increases with time due to gravitational acceleration such that by the time of collapse $\dot{\mu} \sim 120 M_{\odot} \text{ pc}^{-1} \text{ Myr}^{-1}$. Observations have shown that accretion rates on to filaments lie in the range $10\text{--}150 M_{\odot} \text{ pc}^{-1} \text{ Myr}^{-1}$ (Kirk et al. 2013; Palmeirim et al. 2013), thus one cannot realistically invoke higher accretion rates to produce additional turbulence to stabilize nearby supercritical filaments against radial collapse.

However, while the initially sub- and transonic filaments do radially collapse and produce narrow filaments, the initially supersonic filaments are thermally supercritical at the end of the simulations but still show a large radial extent. Fig. 17(a) shows the azimuthally and longitudinally averaged radial volume density profiles for the three natural-mix turbulent cases with initially sub-, tran- and supersonic velocity dispersions, at the end of the simulations when the filaments have line-densities $\sim 1.3 \mu_{\text{CRT}}$. The median was used to average the profile so as to avoid undue influence of outliers, namely the very high density cores. One can see that the initially supersonic case shows the broadest radial profile. The full width

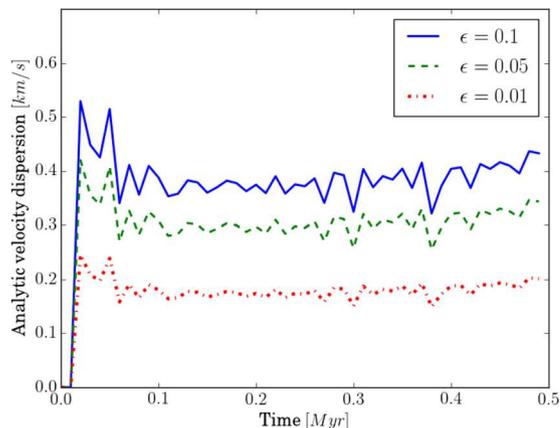


Figure 16. Analytically estimated velocity dispersion due to driving by accretion for the subsonic natural-mix turbulence simulations (equation 11). A driving efficiency between 5 and 10 per cent is necessary to produce a velocity dispersion $\sim 0.4 \text{ km s}^{-1}$ as seen in the simulations.

at half-maxima (FWHMs) of these profiles are, <0.02 , <0.02 and 0.08 pc for the sub-, tran- and supersonic cases respectively. The sub- and transonic cases have upper limits as the resolution of the grid used to produce these plot is 0.01 pc . The same result is seen in column density (Fig. 17b). The FWHMs of the column density profiles are, <0.02 , 0.02 and 0.12 pc for the sub-, tran- and supersonic cases respectively.

The fact that filaments growing from gas with supersonic turbulence do not collapse radially when their line-density exceeds the critical value cannot be attributed to their internal velocity dispersion, since all three cases end up with roughly the same level of internal turbulence. The main difference between the three cases is the resulting morphology; it is possible that the considerable level of sub-structure in the supersonic cases helps to moderate the global

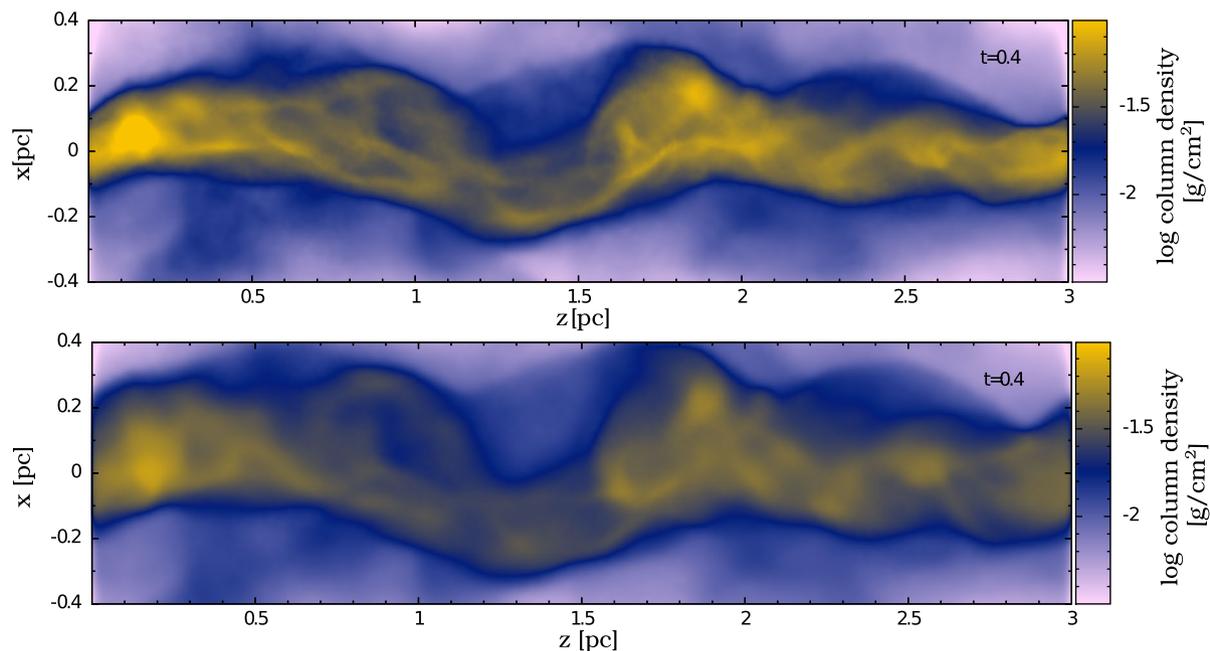


Figure 15. Column density plots of two natural-mix, initially supersonic turbulence simulations that have the same initial conditions. The top panel shows the simulation with self-gravity, and the bottom panel shows the simulation without self-gravity. One can see that both simulations show the same elongated sub-structure, but the sub-structures are more well defined when self-gravity is included. Thus the velocity field is the dominant mechanism for the formation of these fibre-like structures, gravity acts against dispersal but is not necessary for their formation.

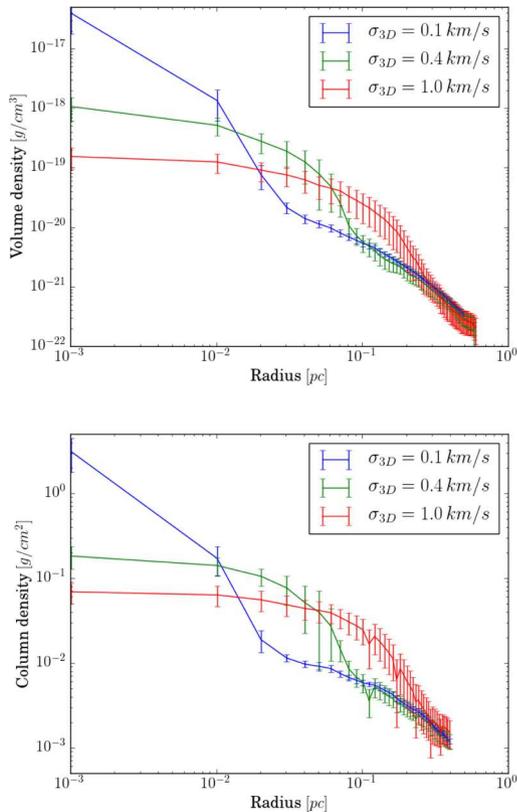


Figure 17. (a) The azimuthally averaged radial volume density profiles for the three natural-mix turbulent cases, initially sub-, tran- and supersonic velocity dispersions, at the end of the simulations when the filaments have line-densities $\sim 1.3\mu_{\text{CRIT}}$. (b) The longitudinally averaged radial column density profiles for the same simulations. The error bars show the inter-quartile range around the median.

radial instability. Possibly the breakup of a filament into fibre-like structures invalidates the assumptions underlying the derivation of the critical line-density in Ostriker (1964); this needs to be investigated further, as it presents a possible solution to the problem that supercritical filaments should collapse radially to widths narrower than the observed 0.1 pc (Arzoumanian et al. 2011; André et al. 2016).

5 CONCLUSIONS

The process by which a filament fragments into cores is complicated by the presence of turbulence and inhomogeneous accretion. Moreover, the amount of turbulence and inhomogeneity produces significant differences in filament morphology and fragmentation.

Filaments fragment gravitationally if they formed in a roughly sub-sonic turbulent and mildly inhomogeneous medium, or where gravity dominates over turbulence, and they show hierarchical two-tiered fragmentation, similar to the fragmentation seen in Orion (Kainulainen et al. 2016b; Teixeira et al. 2016). The first fragments are large-scale structures with wide separations; this fragmentation process is due to the gravitational fragmentation of the filament and is described by a modified dispersion relation derived in CWH16 (their equation 8). Next, these fragments undergo further fragmentation producing small-scale separations; this fragmentation process occurs on the local Jeans length. This change in fragmentation behaviour on different length scales has been seen in G11 by Kainulainen et al. (2013). Moreover, the fragmentation due to Jeans'

instability occurs on a very short time-scale, ~ 0.1 Myr, and removes obvious signs of periodicity in the separation of fragments along a filament, possibly explaining why observed quasi-periodically fragmenting filaments are rare.

As the level of turbulence increases, gravity-dominated filament fragmentation lessens in importance and the fragmentation length scales are mainly determined by the density perturbations delivered by the turbulence. As well as changing fragmentation length scales, increased turbulence causes elongated fibre-like structures to form within the main filament, which is reminiscent of the *fray and fragment* scenario of fibre production *in situ* proposed by Tafalla & Hacar (2015). We see that these structures are intimately linked to the velocity field in the filament. Where there exists a large gradient in vorticity, the velocity field is able to gather gas together and form dense structures. We propose that this vorticity is generated by the radial accretion of an inhomogeneous accretion flow. The radial accretion of gas generates vorticity primarily in the longitudinal direction, thus ‘fraying’ the filament into numerous fibre-like structures.

One could expect that, as fibres accrete from the gas within the filament, which is less turbulent than the gas in the accretion flow, they might fragment in a manner similar to the filaments in the initially sub-sonic simulations. Fibres could therefore be expected to fragment in a quasi-periodic manner. However, the simulations presented here do not contain enough mass for this to occur.

Although the initial level of turbulence in these simulations differs by a factor of 10, the internal filament velocity dispersion always tends towards the sonic level and remains stable until collapse begins. We show that accretion driving is able to sustain this level of turbulence if one takes an efficiency factor of 5–10 per cent. One sees that despite the same level of internal velocity dispersion the filaments in the initially supersonic simulations do not collapse radially when their line-density exceeds the critical value, unlike the initially sub- and transonic cases that do collapse radially. It is possible that the considerable level of sub-structure present means that the fibre-like structures may collapse locally once they become supercritical, whilst the parent filament does not necessarily collapse globally.

The formation, evolution and fragmentation of fibre-like structures will be studied in more detail in future work using simulations that include time-dependent chemistry with coupled heating and cooling (as described in Glover & Clark 2012). These simulations will include realistic thermodynamics, and will allow us to produce synthetic observations to determine if the fibre-like structures seen in PPP space are comparable to the fibres observers see in PPV space. As dendrograms constructed using column density are unable to adequately distinguish large differences in filament sub-structure in PPP space, these synthetic observations will also enable us to investigate the use of dendrograms in PPV space.

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APPENDIX A: SINK IMPLEMENTATION

The standard sink creation criteria invoked in Hubber et al. (2013) are as follows:

- (i) The candidate SPH particle must have a density greater than a pre-defined sink creation density, ρ_{SINK} .
- (ii) The candidate SPH particle must have the lowest gravitational potential of all of its neighbours, i.e. be the local gravitational potential minimum.
- (iii) The candidate SPH particle's smoothing kernel must not overlap with existing sink particles' accretion radii. This prevents overlapping sink particle's forming.
- (iv) The candidate SPH particle must have a density greater than ρ_{HILL} , which is given by

Table A1. A table showing the effect the sink creation density, ρ_{SINK} , has on the time the first sink particle forms, t_{sink} , its position along the filament, z_{sink} , and the number of sinks at the end of simulation, N_{sink} . Note that the third column has two entries for a sink creation density of $10^{-17} \text{ g cm}^{-3}$, this is because two separate sinks form in the same snapshot.

$\rho_{\text{SINK}} (\text{g cm}^{-3})$	$t_{\text{sink}} (\text{Myr})$	$z_{\text{sink}} (\text{pc})$	N_{sink}
10^{-12}	0.629	0.234	11
10^{-13}	0.629	0.234	11
10^{-14}	0.628	0.234	11
10^{-15}	0.627	0.234	11
10^{-16}	0.617	0.235	20
10^{-17}	0.568	0.122/0.235	62

$$\rho_{\text{HILL}} = -\frac{3(\underline{r}_{ij} \cdot \underline{a}_{ij})}{\pi G |\underline{r}_{ij}|^2}, \quad (\text{A1})$$

where \underline{r}_{ij} is the position vector between the candidate SPH particle i and an already existing sink particle j , and \underline{a}_{ij} is the acceleration vector between the two. This criterion allows an extended condensate that already has a sink particle in it to fragment only if the candidate SPH particle is a density peak that dominates the local gravitational field.

These criteria are similar to those used in other implementations in both SPH (Bate, Bonnell & Price 1995; Jappens et al. 2005) and grid codes (Krumholz, McKee & Klein 2004; Federrath et al. 2010a).

Since a new sink creation criterion has been introduced, we run a convergence test to show our choice of ρ_{SINK} is appropriate. Presented in Table A1 is the time the first sink formed, its position along the filament and the number of sinks at the end of the simulation. One can see that above the sink creation $\rho_{\text{SINK}} > 10^{-15} \text{ g cm}^{-3}$, the sinks are well converged.

APPENDIX B: RESOLUTION STUDY

To study the effect that the numerical resolution of the simulation has on the fragmentation, we varied the number of SPH particles for a simulation with $\sigma_{3\text{D}} = 0.1 \text{ km s}^{-1}$ and $\delta_{\text{sol}} = 2/3$. To increase the effective resolution by a factor of 2, one needs to increase the number of particles by 8. Table B1 shows the time the first sink formed, its position along the filament and the number of sinks at the end of the simulation. The number of sinks formed does not change as the resolution increases above 450 000 particles, and the position and time of the first sink changes by <2 percent. Below 450 000 particles both the position of the first sink is different and the number of sinks formed increases. We are thus satisfied that these simulations are converged with 450 000 particles.

Table B1. A table showing the effect the number of particles, N_{SPH} , has on the time the first sink particle forms, t_{sink} , its position along the filament, z_{sink} , and the number of sinks at the end of simulation, N_{sink} . One can see that it has very little effect once the resolution is above 450 000 particles.

N_{SPH}	$t_{\text{sink}} (\text{Myr})$	$z_{\text{sink}} (\text{pc})$	N_{sink}
112 500	0.638	0.061	13
225 000	0.621	0.062	16
450 000	0.627	0.234	11
900 000	0.633	0.234	11
1800 000	0.638	0.231	11
3600 000	0.640	0.233	11

APPENDIX C: SUMMARY OF SINK PROPERTIES

Below are tables detailing the results of all 60 individual simulations. We present the time at which the first sink formed, t_{sink} , the

time the simulation ended when 10 per cent of the mass is in the form of sinks, $t_{10 \text{ per cent}}$, the difference between these times, Δt , and the number of sinks formed by the end of the simulation, N_{sink} , for simulations with initially subsonic (Table C1), transonic (Table C2) and supersonic (Table C3) turbulence.

Table C1. A table showing the time at which the first sink formed, t_{sink} , the time the simulation ended when 10 per cent of the mass is in the form of sinks, $t_{10 \text{ per cent}}$, the difference between these times, Δt , and the number of sinks formed by the end of the simulation, N_{sink} , for each simulation with an initial sub-sonic velocity dispersion of $\sigma_{3D} = 0.1 \text{ km s}^{-1}$. Also shown is the mean and standard deviation of these statistics.

Seed	Natural mix				Purely compressive			
	t_{sink}	$t_{10 \text{ per cent}}$	Δt	N_{sink}	t_{sink}	$t_{10 \text{ per cent}}$	Δt	N_{sink}
1	0.627	0.697	0.070	11	0.594	0.676	0.082	8
2	0.617	0.691	0.074	17	0.599	0.651	0.052	10
3	0.564	0.632	0.068	10	0.579	0.650	0.071	10
4	0.624	0.690	0.066	12	0.589	0.651	0.062	10
5	0.620	0.681	0.061	11	0.590	0.658	0.068	9
6	0.630	0.675	0.045	8	0.587	0.655	0.068	11
7	0.621	0.693	0.072	13	0.620	0.661	0.041	14
8	0.615	0.695	0.080	14	0.603	0.664	0.061	14
9	0.651	0.697	0.046	11	0.603	0.659	0.056	14
10	0.607	0.674	0.067	10	0.608	0.658	0.050	12
Mean	0.618	0.683	0.065	11.7	0.597	0.658	0.061	11.2
σ	0.021	0.019	0.011	2.4	0.011	0.007	0.011	2.1

Table C2. A table showing the time at which the first sink formed, t_{sink} , the time the simulation ended when 10 per cent of the mass is in the form of sinks, $t_{10 \text{ per cent}}$, the difference between these times, Δt , and the number of sinks formed by the end of the simulation, N_{sink} , for each simulation with an initial sonic velocity dispersion of $\sigma_{3D} = 0.4 \text{ km s}^{-1}$. Also shown is the mean and standard deviation of these statistics.

Seed	Natural mix				Purely compressive			
	t_{sink}	$t_{10 \text{ per cent}}$	Δt	N_{sink}	t_{sink}	$t_{10 \text{ per cent}}$	Δt	N_{sink}
1	0.606	0.748	0.142	12	0.557	0.689	0.132	8
2	0.593	0.712	0.119	19	0.540	0.662	0.122	10
3	0.472	0.776	0.304	4	0.514	0.634	0.120	3
4	0.610	0.689	0.079	14	0.520	0.690	0.170	12
5	0.646	0.721	0.075	9	0.508	0.633	0.125	15
6	0.610	0.724	0.114	10	0.570	0.689	0.119	10
7	0.641	0.734	0.093	10	0.655	0.736	0.081	13
8	0.607	0.704	0.097	13	0.569	0.705	0.136	11
9	0.702	0.776	0.074	12	0.528	0.642	0.114	10
10	0.588	0.687	0.099	16	0.611	0.689	0.078	12
Mean	0.608	0.727	0.120	11.9	0.557	0.678	0.120	10.4
σ	0.055	0.030	0.065	3.9	0.044	0.032	0.025	3.1

Table C3. A table showing the time at which the first sink formed, t_{sink} , the time the simulation ended when 10 per cent of the mass is in the form of sinks, $t_{10 \text{ per cent}}$, the difference between these times, Δt , and the number of sinks formed by the end of the simulation, N_{sink} , for each simulation with an initial supersonic velocity dispersion of $\sigma_{3D} = 1.0 \text{ km s}^{-1}$. Also shown is the mean and standard deviation of these statistics.

Seed	Natural mix				Purely compressive			
	t_{sink}	$t_{10 \text{ per cent}}$	Δt	N_{sink}	t_{sink}	$t_{10 \text{ per cent}}$	Δt	N_{sink}
1	0.652	0.864	0.212	13	0.684	0.811	0.127	9
2	0.665	0.793	0.128	20	0.661	0.735	0.084	12
3	0.436	0.658	0.222	7	0.469	0.585	0.116	11
4	0.695	0.859	0.164	13	0.532	0.718	0.186	13
5	0.911	1.027	0.116	23	0.565	0.693	0.128	12
6	0.801	0.867	0.066	11	0.453	0.641	0.188	9
7	0.730	0.847	0.117	16	0.836	0.892	0.056	9
8	0.684	0.820	0.136	7	0.688	0.814	0.126	18
9	0.930	1.010	0.080	3	0.516	0.659	0.143	13
10	0.661	0.725	0.064	14	0.701	0.837	0.136	10
Mean	0.717	0.847	0.131	12.7	0.611	0.739	0.128	11.6
σ	0.134	0.107	0.052	5.8	0.116	0.093	0.039	2.6

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